- (a) Construct the 4 × 4 matrix that corresponds to a 45 degree counter-clockwise rotation around the X − axis followed by a translation by (1,0,0).
 - (b) Given a unit cube with corners (0, 0, 0) and (1, 1, 1), what is the translation of its corners (give all eight coordinates).
- 2. Affine transformations can be represented by 4×4 homogeneous matrices with the following shape:

| Γ | \mathbf{M} | \mathbf{t} | 1 |
|---|--------------|--------------|---|
| L | 0 | 1 | |

where M is a 3×3 matrix and t is a vector. We can use $\langle M | t \rangle$ as a more compact notation for this class of matrices. The product of two homogeneous matrices is

$$\langle \mathbf{M}_1 \mid \mathbf{t}_1 \rangle \langle \mathbf{M}_2 \mid \mathbf{t}_2 \rangle = \langle \mathbf{M}_1 \mathbf{M}_2 \mid \mathbf{M}_1 \mathbf{t}_2 + \mathbf{t}_1 \rangle$$

and applying the transformation to a homogeneous point is

$$\langle \mathbf{M} \mid \mathbf{t} \rangle \begin{bmatrix} \mathbf{v} \\ 1 \end{bmatrix} = \mathbf{M}_1 \mathbf{v} + \mathbf{t}$$

If we restrict ourselves to isotropic (uniform) scaling, rotation, and translation, then these matrices are called *SRT* transforms and have the form $\langle s\mathbf{R} | \mathbf{t} \rangle$, where s is a scalar and **R** is a rotation matrix. Given this notation, solve the following equations:

- (a) $\langle s_1 \mathbf{R}_1 | \mathbf{t}_1 \rangle \langle s_2 \mathbf{R}_2 | \mathbf{t}_2 \rangle$ (b) $\langle s \mathbf{R} | \mathbf{t} \rangle \begin{bmatrix} \mathbf{v} \\ 1 \end{bmatrix}$ (c) $\langle s \mathbf{R} | \mathbf{t} \rangle^{-1}$
- 3. Given a ray $R(t) = \mathbf{o} + t\mathbf{d}$, and a cone whose radius is r and height is h with its base centered at the origin of the X Y plane and its apex at $\langle 0, 0, h \rangle$, what is the polynomial whose roots determine the intersection points of R(t) with the cone?