Why Standard ML?

A language particularly suited to compiler implementation.

- Efficiency
- Safety
- Simplicity
- Higher-order functions
- Static type checking with type inference
- Polymorphism
- Algebraic types and pattern matching
- Modularity
- Garbage collection
- Exception handling
- Libraries and tools

Using the SML/NJ Compiler

- *Type "`sml`" to run the SML/NJ compiler*

  Installed in /usr/local/bin on Linux machines.

- `Cntl-d` *exits the compiler,* `Cntl-c` *interrupts execution.*

- *Three ways to run ML programs:*

  1. type in code in the interactive read-eval-print loop
  2. edit ML code in a file, say `foo.sml`, then type command

     ```
     use “foo.sml”;
     ```

  3. use Compilation Manager (CM):

     ```
     CM.make “sources.cm”;
     ```

ML Tutorial 1

Expressions

- *Integers:* `3, 54, ~3, ~54`
- *Reals:* `3.0, 3.14159, ~3.2E2`
- *Overloaded arithmetic operators:* `+, -, *, /, <, <=`
- *Booleans:* `true, false, not, orelse, andalso`
- *Strings:* `"abc", “hello world\n”, x^".sml"`
- *Lists:* `[], [1,2,3], ["x","str"], 1::2::nil`
- *Tuples:* `(), (1,true), (3,"abc",true)`
- *Records:* `{a=1,b=true}, {name="fred",age=21}`
- *conditionals, function applications, let expressions, functions*

ML Tutorial 2

Declarations: *binding a name to a value*

value bindings

```
val x = 3
val y = x + 1
```

function bindings

```
fun fact n =
    if n = 0 then 1
    else n * fact(n-1)
```

Let expressions: *local definitions*

```
let decl in expr end
```

```
let val x = 3
    fun f y = (y, x*y)
 in f(4+x)
end
```

ML Tutorial 3

Function expressions

The expression "`fn var => exp`" denotes a function with formal parameter *var* and body *exp*.

```
val inc = fn x => x + 1
```

is equivalent to

```
fun inc x = x + 1
```

ML Tutorial 4

Compound values

Tuples: `(exp`$_1$`, ... , exp`$_n$`)`

```
(3, 4.5)

val x = (”foo”, x*1.5, true)
val first = #1(x)

val third = #3(x)
```

Records: `{lab`$_1$` = exp`$_1$`, ... , lab`$_n$` = exp`$_n$`}`

```
val car = {make = “Ford”, year = 1910}

val mk = #make car

val yr = #year car
```

ML Tutorial 5

Patterns

a form to decompose compound values, commonly used in value bindings and function arguments

```
val pat = exp              fun f(pat) = exp
```

variable patterns:

```
val x = 3
⇒ x = 3
fun f(x) = x+2
```

tuple and record patterns:

```
val pair = (3,4.0)
val (x,y) = pair
⇒ x = 3, y = 4.0

val {make=mk, year=yr} = car
⇒ mk = “Ford”, yr = 1910
```

ML Tutorial 6

Patterns

wildcard pattern: `_` *(underscore)*

constant patterns: `3, "a"`

```
fun iszero(0) = true
  | iszero(_) = false
```

constructor patterns:

```
val list = [1,2,3]

val fst::rest = list
⇒ fst = 1, rest = [2,3]
val [x,_,y] = list

⇒ x = 1, y = 3
```

ML Tutorial 7

Pattern matching

match rule: *`pat`* **`=>`** *`exp`*

match: pat_1 **`=>`** exp_1 `| ... |` pat_n **`=>`** exp_n

When a match is applied to a value v, we try rules from left to right, looking for the first rule whose pattern matches v. We then bind the variables in the pattern and evaluate the expression.

case expression: **`case`** *`exp`* **`of`** *`match`*
function expression: **`fn`** *`match`*
clausal functional defn: **`fun`** `f` pat_1 `=` exp_1
`|` `f` pat_2 `=` exp_2
`| ...`
`|` `f` pat_2 `=` exp_2

ML Tutorial 8

Pattern matching examples *(function definitions)*

```
fun length l = (case l
     of [] => 0
      | [a] => 1
      | _ :: r => 1 + length r
    (* end case *))

fun length [] = 0
  | length [a] = 1
  | length (_ :: r) = 1 + length r

fun even 0 = true
  | even n = odd(n-1)

and odd 0 = false
  | odd n = even(n-1)
```

ML Tutorial 9

Types

basic types: `int, real, string, bool`

`3 : int,  true : bool,  “abc” : string`

function types: t_1 `->` t_2

`even: int -> bool`

product types: t_1 `*` t_2 `, unit`

`(3,true): int * bool,  (): unit`

record types: $\{lab_1 : t_1, \ldots, lab_n : t_n\}$

`car: {make : string, year : int}`

type operators: t `list` *(for example)*

`[1,2,3] : int list`

ML Tutorial 10

Type abbreviations

```
type tycon = ty
```

examples:

```
type point = real * real
type line = point * point
type car = {make: string, year: int}
```

```
type tyvar tycon = ty
```

examples:

```
type ‘a pair = ‘a * ‘a
type point = real pair
```

ML Tutorial 11

Datatypes

datatype *tycon* = con_1 **of** ty_1 | ... | con_n **of** ty_n

This is a *tagged union* of variant types ty_1 through ty_n. The tags are the *data constructors* con_1 through con_n.

The data constructors can be used both in expressions to build values, and in patterns to deconstruct values and discriminate variants.

The “**of** *ty*” can be omitted, giving a nullary constructor.

Datatypes can be *recursive*.

```
datatype intlist = Nil | Cons of int * intlist
```

ML Tutorial 12

Datatype example

```
datatype btree = LEAF
               | NODE of int * btree * btree

fun depth LEAF = 0
  | depth (NODE(_,t1,t2)) =
      max(depth t1, depth t2) + 1

fun insert(LEAF,k) = NODE(k,LEAF,LEAF)
  | insert(NODE(i,t1,t2),k) =
      if k > i then NODE(i,t1,insert(t2,k))
      else if k < i then NODE(i,insert(t1,k),t2)
      else NODE(i,t1,t2)

(* in-order traversal of btrees *)
fun inord LEAF = []
  | inord(NODE(i,t1,t2)) =
      inord(t1) @ (i :: inord(t2))
```

ML Tutorial 13

Representing programs as datatypes

```
type id = string

datatype binop = PLUS | MINUS | TIMES | DIV

datatype stm = SEQ of stm * stm
             | ASSIGN of id * exp
             | PRINT of exp list

and exp = VAR of id
        | CONST of int
        | BINOP of binop * exp * exp
        | ESEQ of stm * exp

val prog =
    SEQ(ASSIGN(”a”,BINOP(PLUS,CONST 5,CONST 3)),
        PRINT[VAR “a”])
```

ML Tutorial 14

Computing properties of programs: size

```
fun sizeS (SEQ(s1,s2)) = sizeS s1 + sizeS s2
  | sizeS (ASSIGN(i,e)) = 2 + sizeE e
  | sizeS (PRINT es) = 1 + sizeEL es

and sizeE (BINOP(_,e1,e2)) = sizeE e1 + sizeE e2 + 2
  | sizeE (ESEQ(s,e)) = sizeS s + sizeE e
  | sizeE _ = 1

and sizeEL [] = 0
  | sizeEL (e::es) = sizeE e + sizeEL es


sizeS prog ⇒ 8
```

Types Review

Primitive types

unit, int, real, char, string, ..., instream, outstream, ...

Composite types

unit, tuples, records
function types

Datatypes

types and n-ary type operators, tagged unions, recursive
nominal type equality
bool, list
user defined: trees, expressions, etc.

Type Abbreviations

types and n-ary type operators
structural type equality

```
type ‘a pair = ‘a * ‘a
```

Type Inference

When defining values (including functions), types do not need to be declared -- they will be inferred by the compiler.

```
- fun f x = x + 1;
val f = fn : int -> int
```

Inconsistencies will be detected as type errors.

```
- if 1<2 then 3 else 4.0;
stdIn:1.1-1.23 Error: types of if branches do not agree
  then branch: int
  else branch: real
  in expression:
    if 1 < 2 then 3 else 4.0
```

Type Inference

In some cases involving record field selections, explicit type annotations (called ascriptions*) may be required*

```
- datatype king = {name: string,
                   born: int,
                   crowned: int,
                   died: int,
                   country: string}

- fun lifetime(k: king) =
=     #died k - #born k;
val lifetime = fn : king -> int

- fun lifetime({born,died,...}: king) =
=     died - born;
val lifetime = fn : king -> int
```

partial record pattern

Polymorphic Types

The most general type is inferred, which may be polymorphic

```
- fun ident x = x;
val ident = fn : ‘a -> ‘a

- fun pair x = (x, x);
val pair = fn : ‘a -> ‘a * ‘a

- fun fst (x, y) = x;
val fst = fn : ‘a * ‘b -> ‘a

- val foo = pair 4.0;
val foo : real * real

- fst foo;
val it = 4.0: real
```

Polymorphic Types

The most general type is inferred, which may be polymorphic

```
- fun ident x = x;
val ident = fn : ‘a -> ‘a

- fun pair x = (x, x);
val pair = fn : ‘a -> ‘a * ‘a

- fun fst (x, y) = x;
val fst = fn : ‘a * ‘b -> ‘a

- val foo = pair 4.0;
val foo : real * real

- fst foo;
val it = 4.0: real
```

type variable

polymorphic type

`: real -> real * real`

Polymorphic Data Structures

```
- infixr 5 ::
- datatype ‘a list = nil
                   | :: of ‘a * ‘a list

- fun hd nil = raise Empty
=     | hd (x::_) = x;
val hd = fn : ‘a list -> ‘a

- fun length nil = 0
=     | length (_::xs) = 1 + length xs;
val length = fn : ‘a list -> int

- fun map f nil = nil
=     | map f (x::xs) = f x :: map f xs;
val map = fn : (’a -> ‘b) -> ‘a list -> ‘b list
```

More Pattern Matching

Layered Patterns: *x* as *pat*

```
(* merging two sorted lists of ints *)
fun merge(x, nil) = x
  | merge(nil, y) = y
  | merge(l as x::xs, m as y::ys) =
      if x < y then x :: merge(xs,m)
      else if y < x then y :: merge(l,m)
      else x :: merge(xs,ys);
val merge = fn : int list * int list -> int list
```

Note: although < is overloaded, this definition is unambiguously typed with the lists assumed to be int lists because the < operator defaults to the int version (of type `int*int->bool`).

Exceptions

```
- 5 div 0;                      (* primitive failure *)
uncaught exception Div

exception NotFound of string;   (* control structure *)
type ‘a dict = (string * ‘a) list
fun lookup (s,nil) = raise (NotFound s)
  | lookup (s,(a,b)::rest) =
      if s = a then b else lookup (s,rest)
val lookup: string * ‘a dict -> ‘a

val dict = [(”foo”,2), (”bar”,~1)];
val dict: string * int list          (* == int dict *)

val x = lookup(”foo”,dict);
val x = 2 : int

val y = lookup(”moo”,dict);
uncaught exception NotFound

val z = lookup(”moo”,dict) handle NotFound s =>
        (print (“can’t find “^s^”\n”); 0)
can’t find moo
val z = 0 : int
```

References and Assignment

```
type ‘a ref
val ref : ‘a -> ‘a ref
val ! : ‘a ref -> ‘a
val := : ‘a ref * ‘a -> unit

val linenum = ref 0;    (* create updatable ref cell *)
val linenum = ref 0 : int ref

fun newLine () = linenum := !linenum + 1;   (* increment it *)
val newline = fn : unit -> unit

fun lineCount () = !linenum;   (* access ref cell *)
val lineCount = fn : unit -> int

local val x = 1
   in fun new1 () = let val x = x + 1 in x end
  end  (* new1 always returns 2 *)

local val x = ref 1
   in fun new2 () = (x := !x + 1; !x)
  end  (* new2 returns 2, 3, 4, ... on successive calls *)
```

Simple Modules -- *Structure*

```
structure Ford =
struct
  type car = {make: string, built: int}
  val first = {make = “Ford”, built: 1904}
  fun mutate ({make,built}: car) year =
      {make = make, built = year}
  fun built ({built,...}: car) = built
  fun show (c) = if built c < built first then “ - ”
                 else “(generic Ford)”
end

structure Year =
struct
  type year = int
  val first = 1900
  val second = 2000
  fun newYear(y: year) = y+1
  fun show(y: year) = Int.toString y
end

structure MutableCar =
struct
  structure C = Ford
  structure Y = Year
end
```

A *structure* is an encapsulated, named, collection of declarations

Module Interfaces -- *Signature*

```
signature MANUFACTURER =
sig
  type car
  val first : car
  val built : car -> int
  val mutate : car -> int -> car
  val show : car -> string
end

signature YEAR =
sig
  eqtype year
  val first : year
  val second : year
  val newYear : year -> year
  val show : year -> string
end

signature MCSIG =
sig
  structure C : MANUFACTURER
  structure Y : YEAR
end
```

A *signature* is a collection of specifications for module components -- types, values, structures

Signature Matching

```
structure Year1 : YEAR =
struct
  type year = int
  type decade = string
  val first = 1900
  val second = 2000
  fun newYear(y: year) = y+1
  fun leap(y: year) = y mod 4 = 0
  fun show(y: year) = Int.toString y
end
```

Structure S *matches* SIG if S if every spec in SIG is matched by a component of S.

S can have more components than are specified in SIG.

```
structure MCar : MCSIG = MutableCar

val classic = Year1.show 1968

val antique = MCar.Y.show 1930

val x = Year1.leap(Year1.first)
```

Use the *dot notation* to access components of structures.

Can’t access components not specified in signature.

Module Functions -- *Functors*

```
signature ORD =
sig
  type t
  val less : t * t -> bool
end

functor Sort(X: ORD) =
struct
  fun insert(x,nil) = [x]
    | insert(x,l as y::ys) =
        if X.less(x,y) then x::l
         else y::insert(x,ys)
  fun sort (m : X.t list) = foldl insert nil m
end
```

`Sort` is a *parameterized module*, with parameter `X: ORD`

```
structure IntOrd : ORD =
struct
  val t = int
  val less = Int.<
end

structure IntSort = Sort(IntOrd)
```

functor application

Input/Output

```
structure TextIO : sig

type instream                         (* an input stream *)
type outstream                        (* an output stream *)

val stdIn : instream                  (* standard input *)
val stdout : outstream                (* standard output *)
val stdErr : outstream                (* standard error *)

val openIn: string -> instream        (* open file for input *)
val openOut: string -> outstream      (* open file for output *)
val openAppend: string -> outstream (* open file for appending *)

val closeIn: instream -> unit         (* close input stream *)
val closeOut: outstream -> unit       (* close output stream *)

val output: outstream * string -> unit (* output a string *)

val input: instream -> string         (* input a string *)
val inputLine: instream -> string option (* input a line *)
.....
end
```

Modules --- type abstraction

Consider the problem of providing *unique* identifiers.

```
signature UID =
  sig
    type uid
    val same : (uid * uid) -> bool
    val compare : (uid * uid) -> order
    val gensym : unit -> uid
  end
```

Modules --- type abstraction

```
structure UId :> UID =
  struct
    type uid = int  (* abstract *)
    fun same (a : uid, b) = (a = b)
    val compare = Int.compare

    val count = ref 0  (* hidden *)
    fun gensym () = let
          val id = !count
          in
            count := id + 1;
            id
          end

  end
```

Readers

The `StringCvt` module defines the reader type, which defines a *pattern* of functional input.

```
type (’item, ‘strm) reader
      = ‘strm -> (’item, ‘strm) option

val scan : (char, ’strm) reader
      -> (ty, ’strm) reader
```

Readers

```
fun skipWS getc = let
      fun skip strm = (case getc strm
             of NONE => strm
              | SOME(c, strm’) =>
                  if (Char.isSpace c)
                    then skip strm’
                    else strm
            (* end case *))
      in
        skip
      end
```

```
val skipWS : (char, ‘strm) reader
      -> ‘strm -> ‘strm
```