Algorithms – CS-27200/37000 Homework – March 2, 2005 Instructor: László Babai Ry-164 e-mail: laci@cs.uchicago.edu

TA SCHEDULE: TA sessions are held in Ryerson-255, Tuesday and Thursday 5–6pm, Saturday 11am–noon, and (this is new) Wednesday after class 12:30–1:20 or 1:30–2:20 depending on demand. Indicate your interest in the Wednesday session to the instructor immediately after class.

TA schedule during exam week: TA sessions will continue through March 18 (final exam) on the same schedule. On Wednesday, March 14, Hari will be available both at 12:30 and at 1:30pm.

ADVICE. Take advantage of the TA sessions.

Check the class <u>website</u>, http://www.classes.cs.uchicago.edu/current/27200-1.

DATES TO REMEMBER: Mon Mar 7: Midterm 2, Fri Mar 11: Last class. ATTENDANCE REQUIRED. Fri Mar 18, 10:30–12:30: Final Exam

19.1 There was a mistake in the statement of Problem 16.3. (The reduction as originally stated went the wrong way.) This is a reassignment of the problem. If you received full score on 16.3, you do not need to hand in a solution to 19.1; you points for 16.3 will be credited toward 19.1. If you did not receive full score on 16.3, please solve 19.1; you will neither gain nor lose points for your solution to 16.3.

Recall that a Cook-reduction of a function $f_1: \Sigma_1^* \to \Pi_1^*$ to a function $f_2: \Sigma_2^* \to \Pi_2^*$ is a polynomial-time algorithm to compute f_1 with "oracle access" to f_2 , i. e., f_1 is permitted to use f_2 as a "subroutine." $(\Sigma_1, \Pi_1, \Sigma_2, \Pi_2 \text{ are finite alphabets.})$ Note that whenever f_1 uses a call to f_2 , the algorithm needs to compute the input to f_2 and read its output; therefore these inputs and outputs must have length, polynomially bounded in the original input length.

- (a) (8 points, G only) Give a Cook-reduction of the problem of finding a 3-coloring of a given graph if a 3-coloring exists (not a decision problem) to the problem of graph-3-colorability (a decision problem).
- (b) (U, G, 3 points) Prove that no such Karp-reduction exists.