Homework 2 January 27, 2009

## Homework 2 Due: February 3, 2009

- 1. Write regular expressions for the following languages:
  - (a) Strings over the alphabet  $\{a, b, c\}$  with exactly 2 bs.
  - (b) Strings over the alphabet {a, b, c} where the first a precedes any occurrence of b and the first b precedes any occurrence of c.
  - (c) Strings over the alphabet  $\{0, 1\}$  that describe binary integers (with no leading zeros) that represent a value of the form  $2^n + 1$ .
- 2. (a)-(c) Draw non-deterministic finite automatons (NFAs) that accept the languages in Problems 1(a)-(c).
- 3. The following RE describes binary numbers (either signed or unsigned and either integer or floating point):

 $(-|\epsilon)(\mathbf{0}|\mathbf{1})^{+}(.(\mathbf{0}|\mathbf{1})^{+})^{?}(\mathbf{E}(\mathbf{+}|\mathbf{-}|\epsilon)(\mathbf{0}|\mathbf{1})^{+})^{?}$ 

(Unlike Problem 1(c), this RE accepts leading zeros.) Draw a non-deterministic finite automata (NFA) that accepts the same language as the above RE.

4. Consider the following NFA over the alphabet {**a**, **b**, **c**}:



- (a) Give the  $\epsilon$ -closure for each state in the NFA.
- (b) Convert the NFA to a DFA using the subset-construction method. (You may omit transitions to the error state (the DFA state corresponding to the empty set of NFA states).)
- (c) Give an RE that defines the same language as the NFA.

## **Document history**

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