

1. Consider a cylinder with radius 1 and height 2 that is centered at the origin with its axis being the Z axis.
  - (a) Give an *implicit* representation of the cylinder.
  - (b) Given a sphere  $\langle \mathbf{c}, r \rangle$ , give pseudo code to determine if the sphere intersects the cylinder. Explain your answer.
2. An *oriented bounding box* (OBB) can be represented by a center point  $\mathbf{p}$ , a 3x3 rotation matrix  $\mathbf{R}$  (the columns of this matrix define the axes of the OBB), and a vector  $\mathbf{s}$  of extents (the distances from the center to the sides along each of the OBB's axes).
  - (a) Define an affine transformation that takes the axis-aligned  $2 \times 2 \times 2$  cube centered at the origin to the OBB.
  - (b) Given a **ray**  $R(t) = \mathbf{o} + t\mathbf{d}$ , with  $\|\mathbf{d}\| = 1$  and  $0 \leq t$ , give pseudo code for an intersection test for the ray and OBB.
3. Assume that we are approximating the circle defined by  $x^2 + y^2 - r^2 = 0$  and  $z = d$  (in eye space) by a regular hexagon that is inscribed in the circle (*i.e.*, the vertices of the hexagon lie on the circle). If the focal length is  $e$ , what is the maximum error in the radius of the approximation in projection-space coordinates.