

# An Invitation to Cryptography

CMSC 23200/33250, Autumn 2018, Lecture 2

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8580	...
8581	...
8582	...
8583	...
8584	...
8585	...
8586	...
8587	...
8588	...
8589	...

6V 断 4.5V



nothing

Today 11:11

Can you please come over  
asap to help me move the  
couch?

I need to be out of here by  
3pm

I guess you forgot your  
phone at home or  
something

Delivered

Send



iMessage







51000

21

5100

N





**The Wi-Fi network "Pat'swifi" requires a WPA2 password.**

Password:

- Show password
- Remember this network



Cancel

Join



### www.amazon.com

Your connection to this site is private.

[Details](#)

Permissions

Connection



Chrome verified that Symantec Class 3 Secure Server CA - G4 issued this website's certificate. The server did not supply any Certificate Transparency information.

[Certificate Information](#)



Your connection to www.amazon.com is encrypted using a modern cipher suite.

The connection uses TLS 1.2.

The connection is encrypted and authenticated using AES\_128\_GCM and uses ECDHE\_RSA as the key exchange mechanism.

[What do these mean?](#)

ON UPDATED DAILY

EXPLORE

amazon

Departments

zon.com

Today's Deals

Gift Cards

DESTINATION  
ENTERTAINMENT

fire \$499



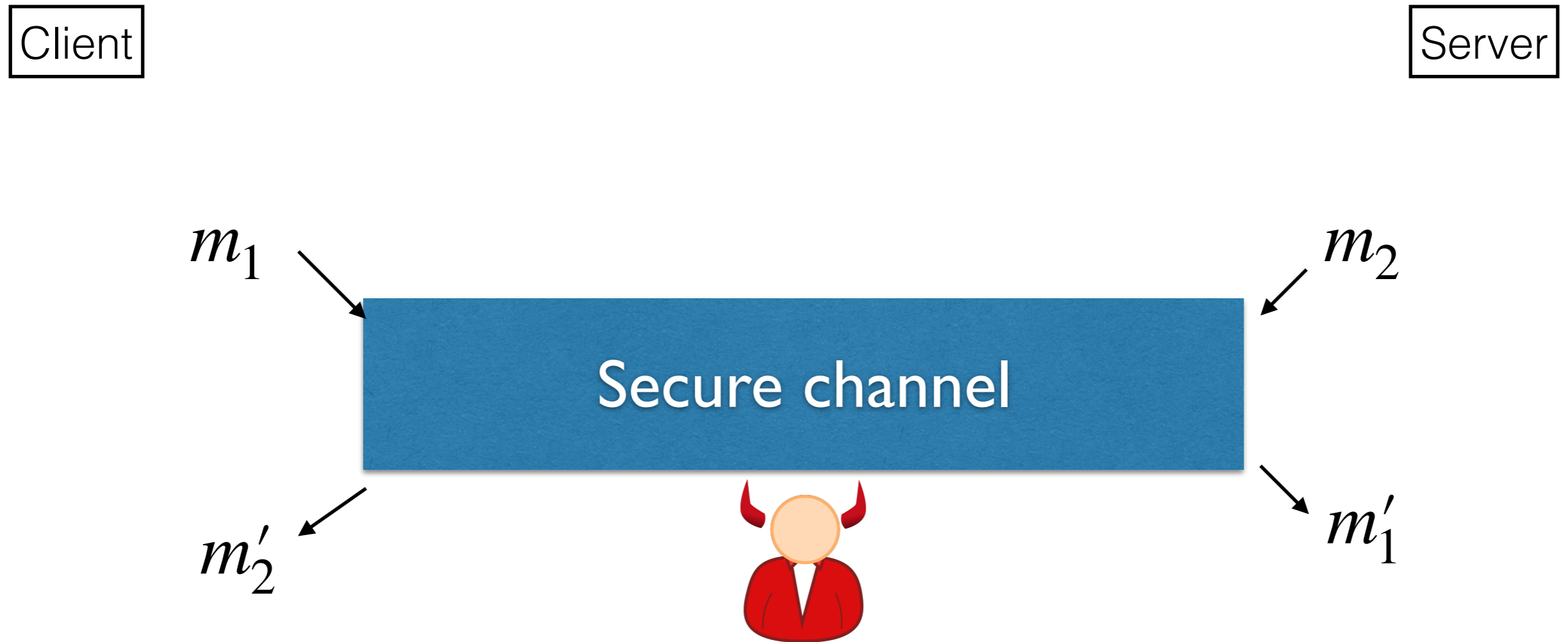
# What is Cryptography?

Cryptography involves algorithms with security goals.

Cryptography involves using math to stop adversaries.



# Common Security Goal: Secure Channel



**Confidentiality:** Adversary does not learn anything about messages  $m_1, m_2$

**Authenticity:**  $m'_1 = m_1$  and  $m'_2 = m_2$



**Warning: subtitles abound**





# WEP/WPA1,2: Secure WiFi

pw="fourwordsuppercase"



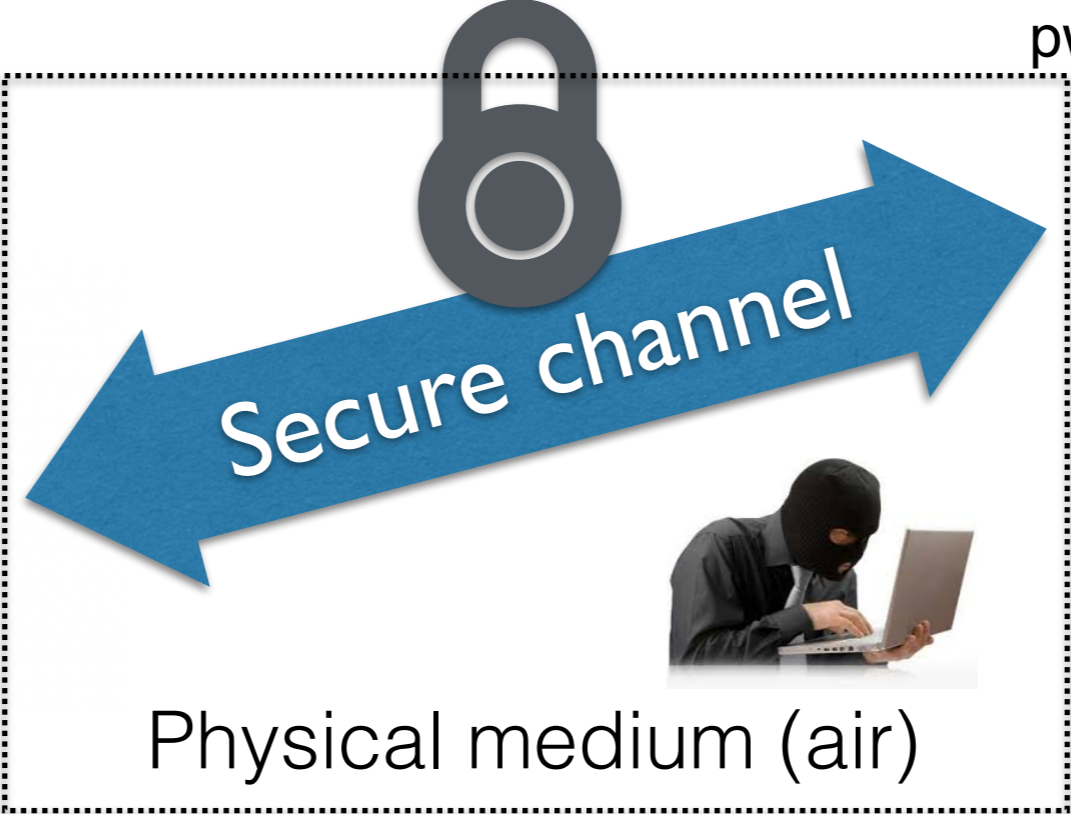
Yo, w ...  
... nevermind

It's four words uppercase,  
one word, lowercase.



# WPA2 (Wi-Fi Protected Access 2): Secure WiFi

pw="fourwordsuppercase"



pw="fourwordsuppercase"

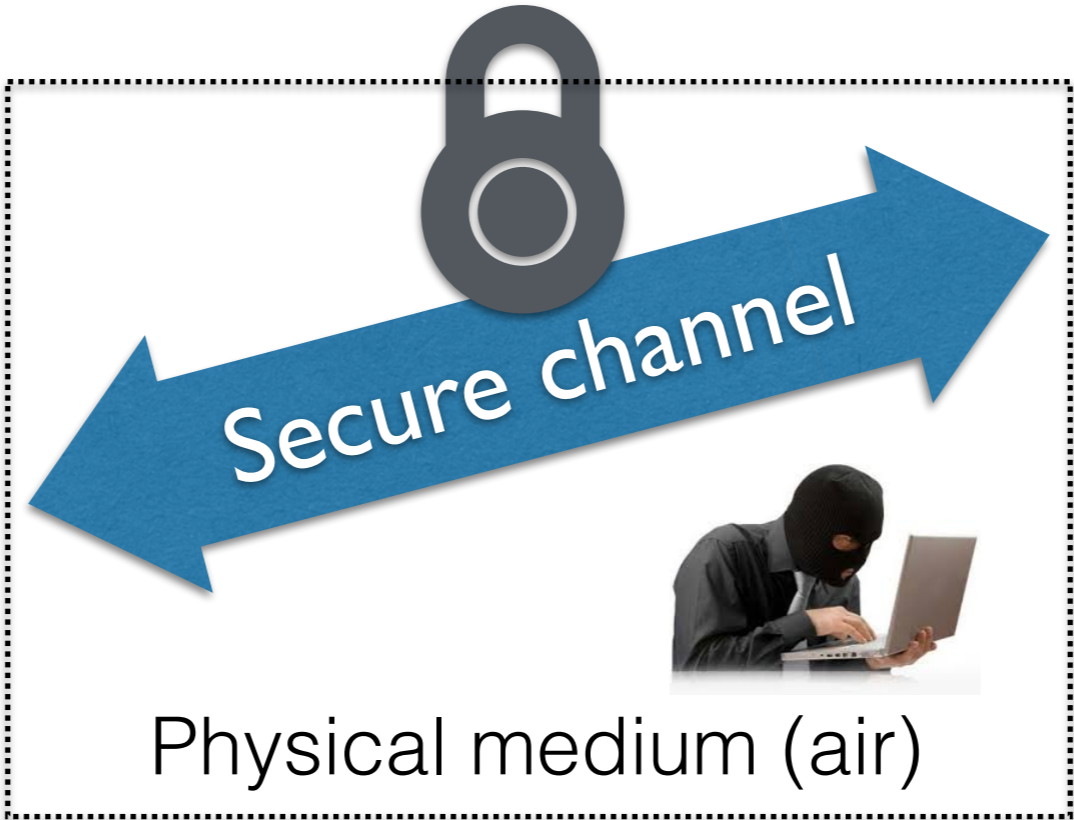




# GSM Cell Phone Encryption (A5/1, A5/3)



$K = b9842544$



User	Key
Alice Doe	340934c3
Betty Lee	b9842544
Cheryl Zang	93d94520
Pat Dobbs	2ea0f48d

...

...

# Crypto in your browser: TLS (Transport Layer Security)



Time to pull the trigger and buy that Boyfriend Pillow I've had my eye on...





# Crypto in your browser: TLS (Transport Layer Security)



Broken by:



Actually TLS seems to work most of the time.

Used billions of times a day, supporting Internet and web.

# Four settings for cryptography

Security Goal	Confidentiality	Authenticity
Pre-shared key?	Symmetric Encryption (aka Secret-key Encryption)	Message Authentication Code (MAC)
Symmetric	Asymmetric Encryption (aka Public-key Encryption)	Digital Signatures

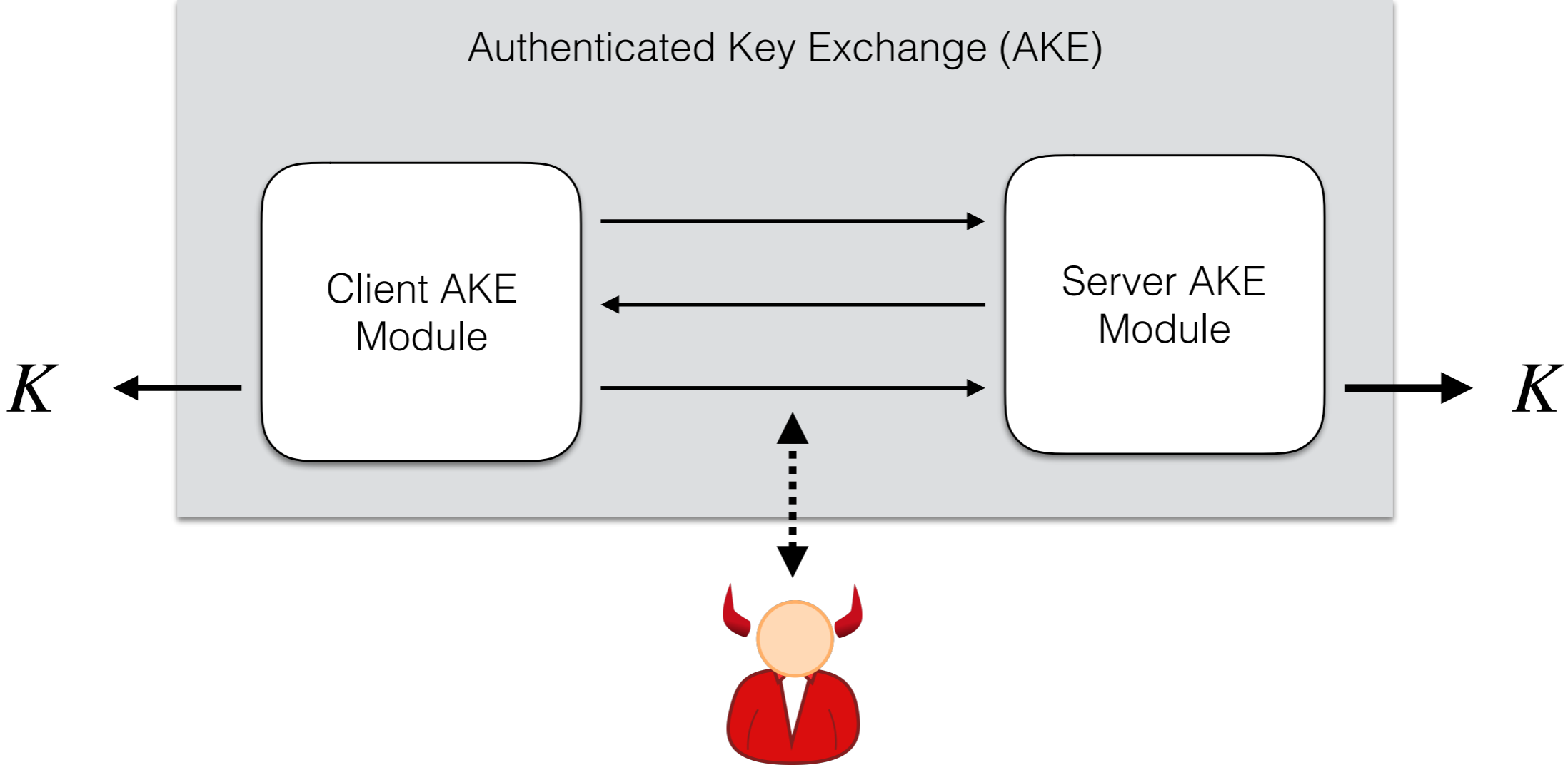
Now: A tour of TLS, which uses all 4.



# TLS Cryptographic Core

Client

Server



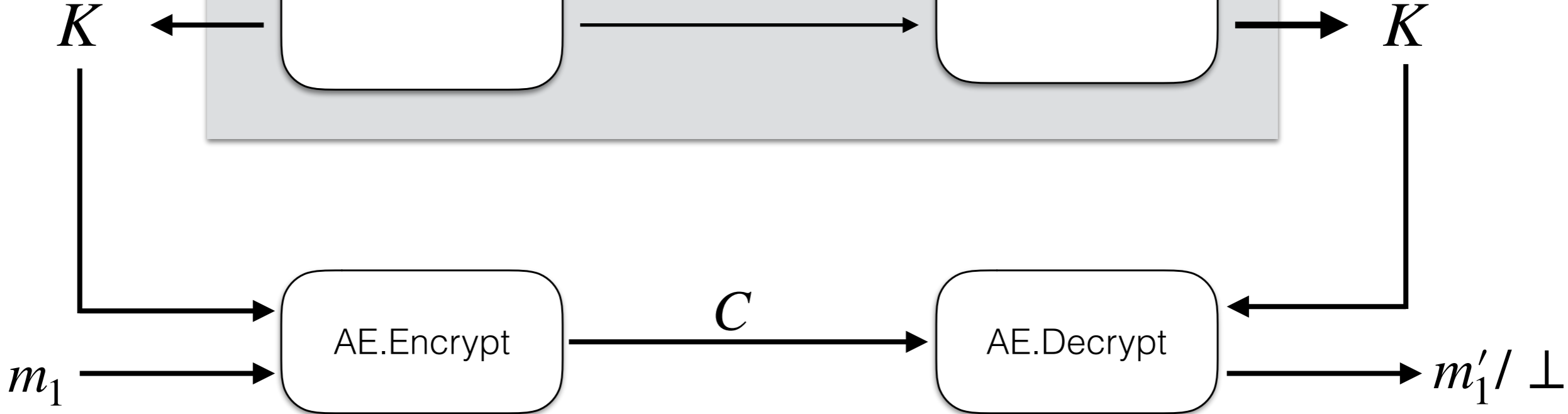
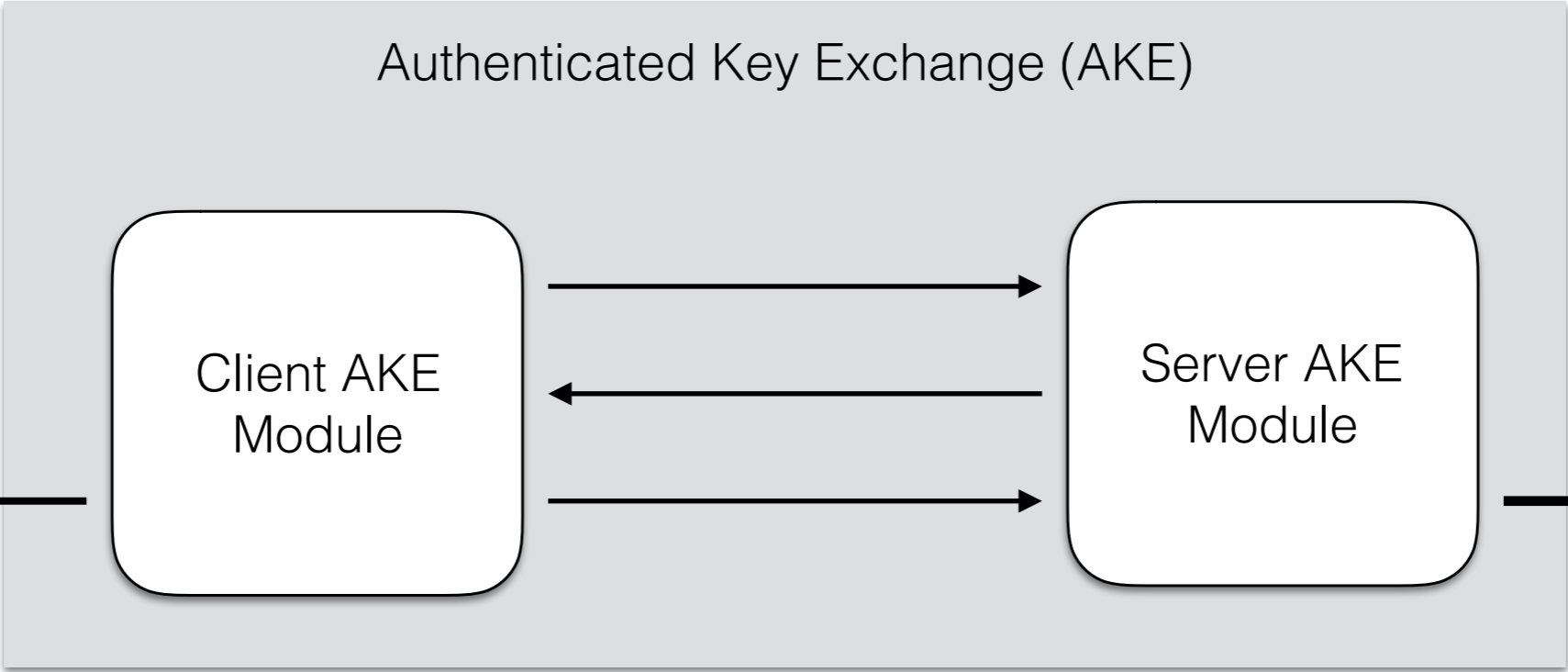
$K$  should be a fresh random and authentic session key

Adversary should not be able to influence or know  $K$

# TLS Cryptographic Core

Client

Server



AE: Authenticated Encryption Scheme  
 $C$ : Ciphertext  
 $\perp$ : ERROR/REJECT



Client



Server

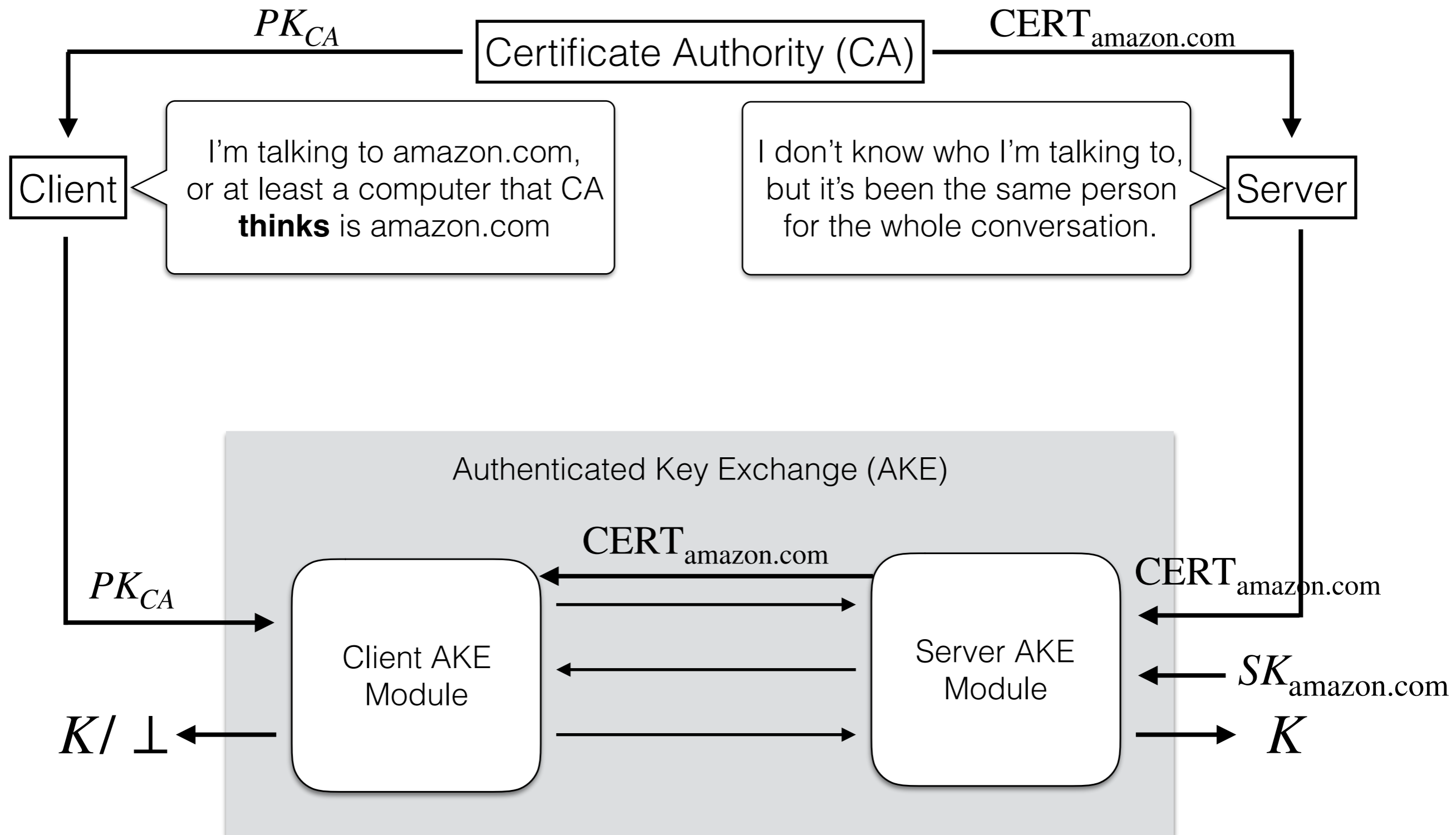
What does it mean to **really** talk to amazon.com?

Messages were emitted by machine owned by Amazon.com Inc.

Messages were emitted by machine with IP address associated to amazon.com by DNS.

I'm getting my boyfriend pillow *like now*.





$CERT_{amazon.com}$  : amazon.com certificate issued by CA  
 $PK_{CA}$  : CA's public key  
 $SK_{amazon.com}$  : amazon.com's secret key tied to  $CERT_{amazon.com}$



# Certificate Authorities



Hundreds more, some with dubious security practices.

8/30/2011  
12:40 PM



Kelly Jackson  
Higgins

## Digital Certificate Authority Hacked, Dozens Of Phony Digital Certificates Issued

DigiNotar confirms it was breached and Google.com just one of 'several dozens' of fraudulently issued digital certificates obtained by hackers and now revoked



**Safari is using an encrypted connection to www.amazon.com.**  
Encryption with a digital certificate keeps information private as it's sent to or from the https website www.amazon.com.

- DigiCert Global Root G2
  - DigiCert Global CA G2
    - www.amazon.com



**www.amazon.com**  
Issued by: DigiCert Global CA G2  
Expires: Friday, March 29, 2019 at 7:00:00 AM Central Daylight Time  
✔ This certificate is valid

- ▶ Trust
- ▼ Details

**Subject Name**

Country US  
State/Province Washington  
Locality Seattle  
Organization Amazon.com, Inc.  
Common Name www.amazon.com

**Issuer Name**

Country US  
Organization DigiCert Inc  
Common Name DigiCert Global CA G2

Serial Number 07 DC 7D 69 44 60 E6 47 B7 6C 6E 78 E8 59 62 00  
Version 3  
Signature Algorithm SHA-256 with RSA Encryption ( 1.2.840.113549.1.1.1 )  
Parameters None

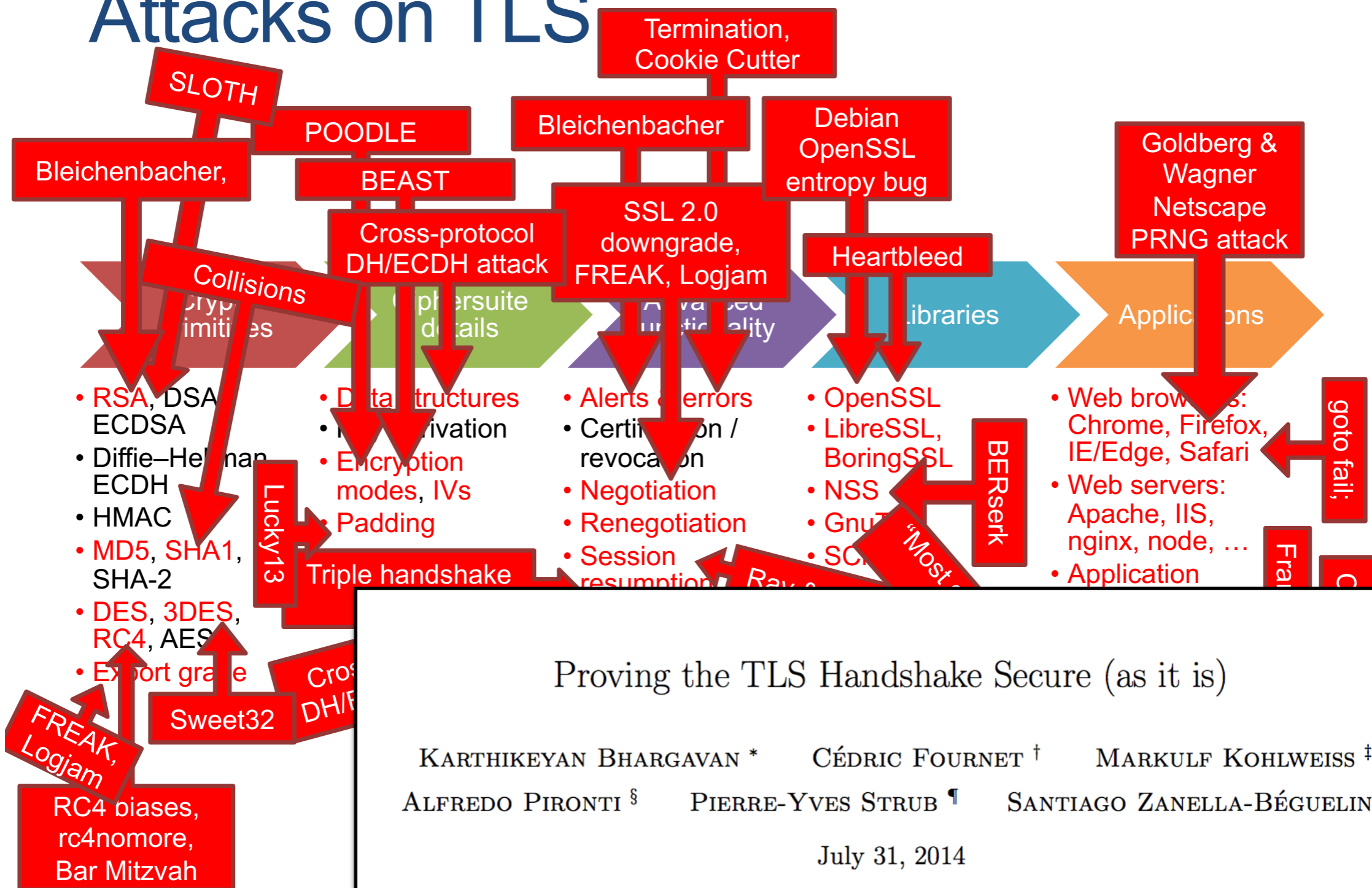
Not Valid Before Tuesday, March 27, 2018 at 7:00:00 PM Central Daylight Time  
Not Valid After Friday, March 29, 2019 at 7:00:00 AM Central Daylight Time

**Public Key Info**

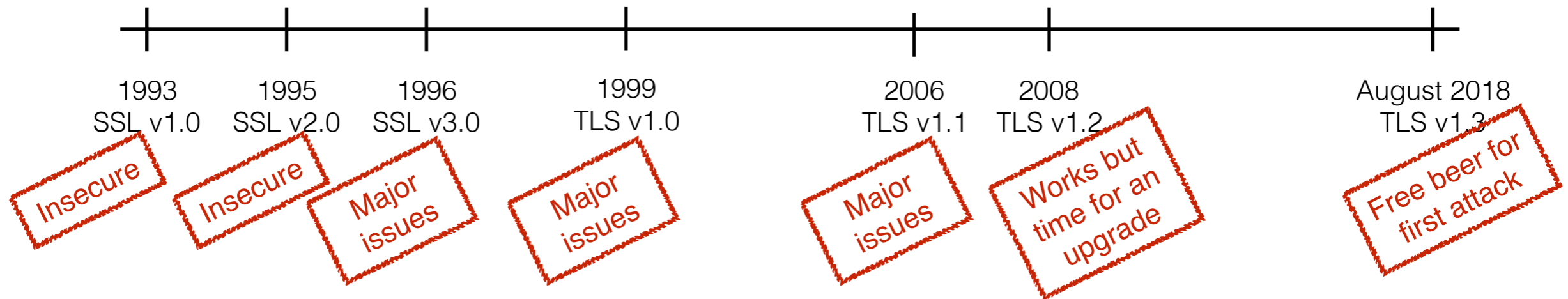
Algorithm RSA Encryption ( 1.2.840.113549.1.1.1 )  
Parameters None  
Public Key 256 bytes : E7 93 5A 5E F0 25 E1 7E 06 DB 88 1D 23 85 8C D0 25 5B 8B F5 51 72 F8 88 79 F5 47 23 F1 7C 2B 03 4D D4 05 42 46 47 A2 6B CC 2F 9E 55 D2 0B 07 C5 D2 84 24 FA 5F A0 AD E3 F0 2F C7 68 1F 93 14 88 A9 06 64 F1 82 05 42 0E 90 D5 D4 6C 52 E4 D6 60 D9 4D 33 19 F2 13 82 9E 1D 13 F0 E2 43 01 DD 42 51 59 83 E9 74 1D 2E 69 A9 41 FC 8B 56 C7 01 AB 1A DE 9D 4C 13 63 65 92 37



# Attacks on TLS



# TLS History



Grandma, TLS 1.3 zero round-trip time session resumption with perfect forward secrecy is soooo dated.

Back in my day we did four-way handshakes... both ways, in the snow! With subgroups of prime fields!

### Security

## It's official: TLS 1.3 approved as standard while spies weep

Now all you lot have to actually implement it

By [Kieren McCarthy](#) in San Francisco 13 Aug 2018 at 22:19 26 [SHARE](#)



First deployments happening now!

overhaul of a critical internet security protocol has been completed, TLS 1.3 becoming an official standard late last week.



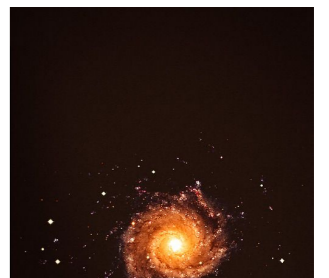
# Crypto tools in TLS

Key Exchange  
Public-Key Encryption  
Trapdoor Function  
Authenticated Encryption  
Blockcipher  
Stream cipher  
Message Authentication Code  
Digital Signature  
Collision-Resistant Hash Function  
...



Every interaction between pieces is an opportunity for an attacker.

Each has unique and subtle security properties  
... all so we can buy boyfriend pillows securely



# Crypto in CSMC 23200

Symmetric Encryption (Lectures 2 & 3)

Symmetric Authentication and Hashing (Lecture 4 and 5)

Asymmetric Encryption (Lecture 6)

Digital Signatures (Lecture 7)

Putting it together: TLS (Lectures 8 & 9)

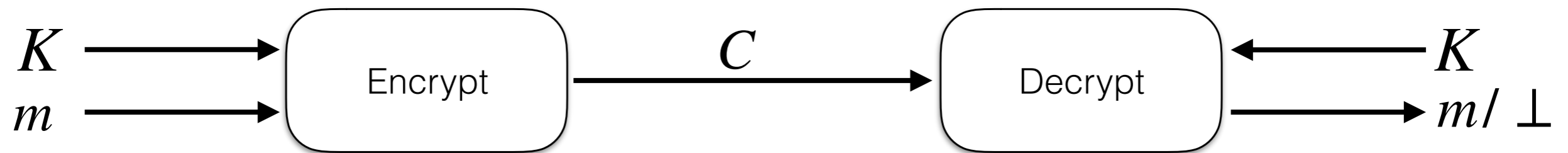


## Rest of this lecture

- Syntax of a cipher
- Some historical ciphers and how they were broken
- The One-Time Pad cipher and its security/insecurity
- Towards practice: Begin stream ciphers and blockciphers

# Cipher Syntax

A cipher is a pair of algorithms Encrypt, Decrypt:



Require that decryption recovers the same message.



# Historical Cipher: ROT13 (“Caesar cipher”)

Encrypt(K,m): shift each letter of plaintext forward by K positions in alphabet (wrap from Z to A).

Plaintext: **DEFGH**

Key (shift): 3

Ciphertext: **FGHKL**

Plaintext: **ATTACKATDAWN**

Key (shift): 13

Ciphertext: **NGGNPXNGQNJJA**

# Historical Cipher: Substitution Cipher

Encrypt(K,m): Parse key K as a permutation  $\pi$  on  $\{A, \dots, Z\}$ .  
Apply  $\pi$  to each character of m.

P: ATTACKATDAWN

K:  $\pi$  

C: ZKKZAMZKYZGT

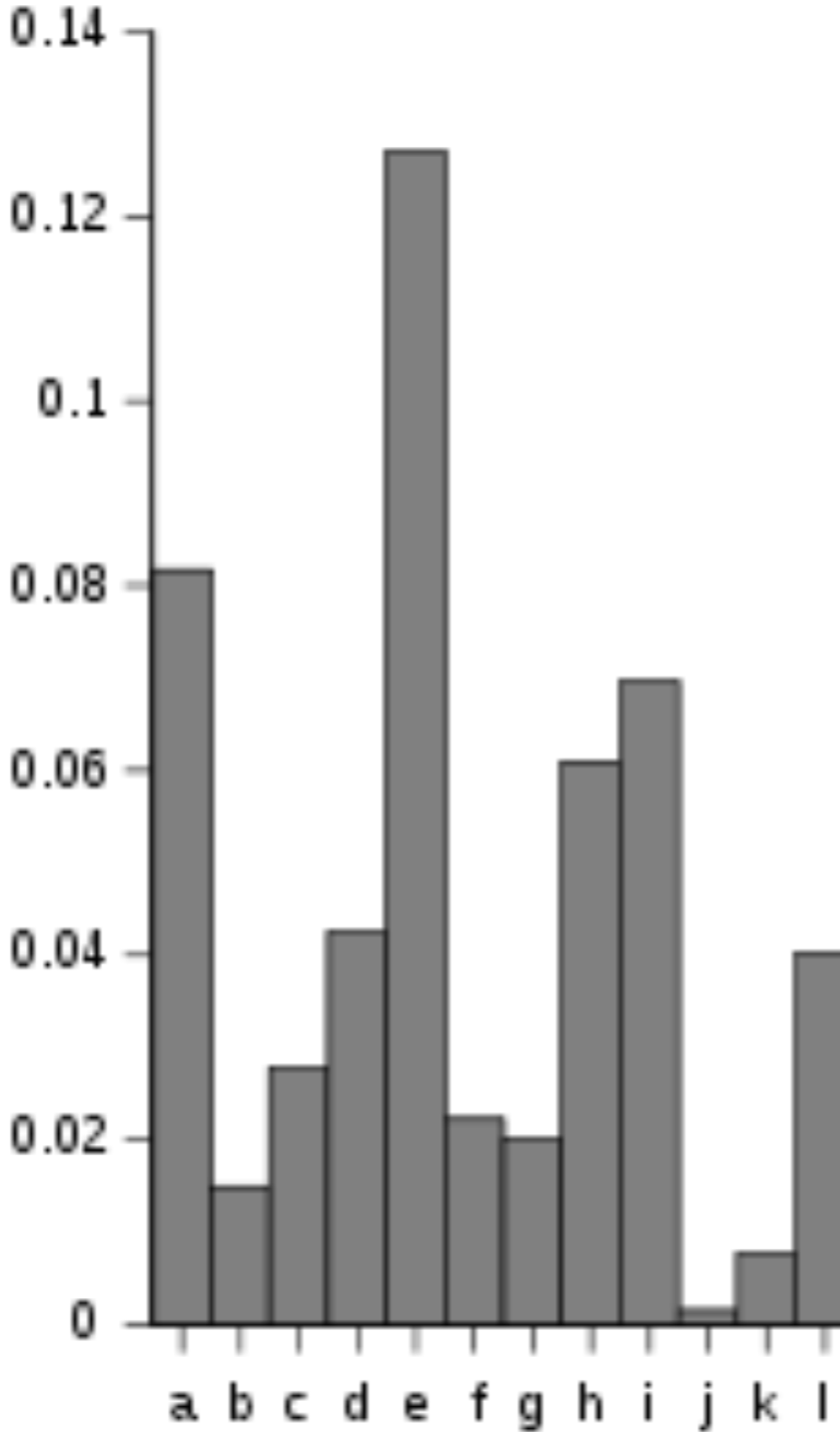
x	$\pi(x)$
A	Z
B	U
C	A
D	Y
E	R
F	E
G	X
H	B
I	D
J	C
K	M
L	Q
M	H
N	T
O	I
P	S
Q	V
R	N
S	P
T	K
U	O
V	F
W	G
X	W
Y	L
Z	J

How many keys?

$$26! \approx 2^{88}$$

9 million years to try all keys at rate of  
1 trillion/sec

# Cryptanalysis of Substitution Cipher



**CELEBRITY CIPHER**  
by Luis Campos

Celebrity Cipher cryptograms are created from quotations by famous people, past and present.  
Each letter in the cipher stands for another.

“ U P X E G T H W Z H F X Y L F H O S L N P F X . H M  
T P J S X E P O X V P G A V G P O S L E E B X X O A  
P M L N P F X , T P J ' C X Z P W E E B X V B P Z X  
E B H O S . ” — V . W . Y X G V H O

Previous Solution: “Time is the cruelest teacher; first she gives the test, then teaches the lesson.” — Leonard Bernstein

*TODAY'S CLUE: r sjænbə N*

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# Quick recall: Bitwise-XOR operation

We will use bit-wise XOR:

$$\begin{array}{r} 0101 \\ \oplus 1100 \\ \hline 1001 \end{array}$$

Some Properties:

$$-X \oplus Y = Y \oplus X$$

$$-X \oplus X = 000\dots 0$$

$$-X \oplus Y \oplus X = Y$$

# Cipher Example: One-Time Pad

Key K: Bitstring of length L

Plaintext M: Bitstring of length L

Encrypt(K,M): Output  $K \oplus M$

Decrypt(K,C): Output  $K \oplus C$

Example:

$$\begin{array}{r} 0101 \\ \oplus 1100 \\ \hline 1001 \end{array}$$

Correctly decrypts because

$$K \oplus C = K \oplus (K \oplus m) = (K \oplus K) \oplus m = m$$

Q: Is the one-time pad secure?

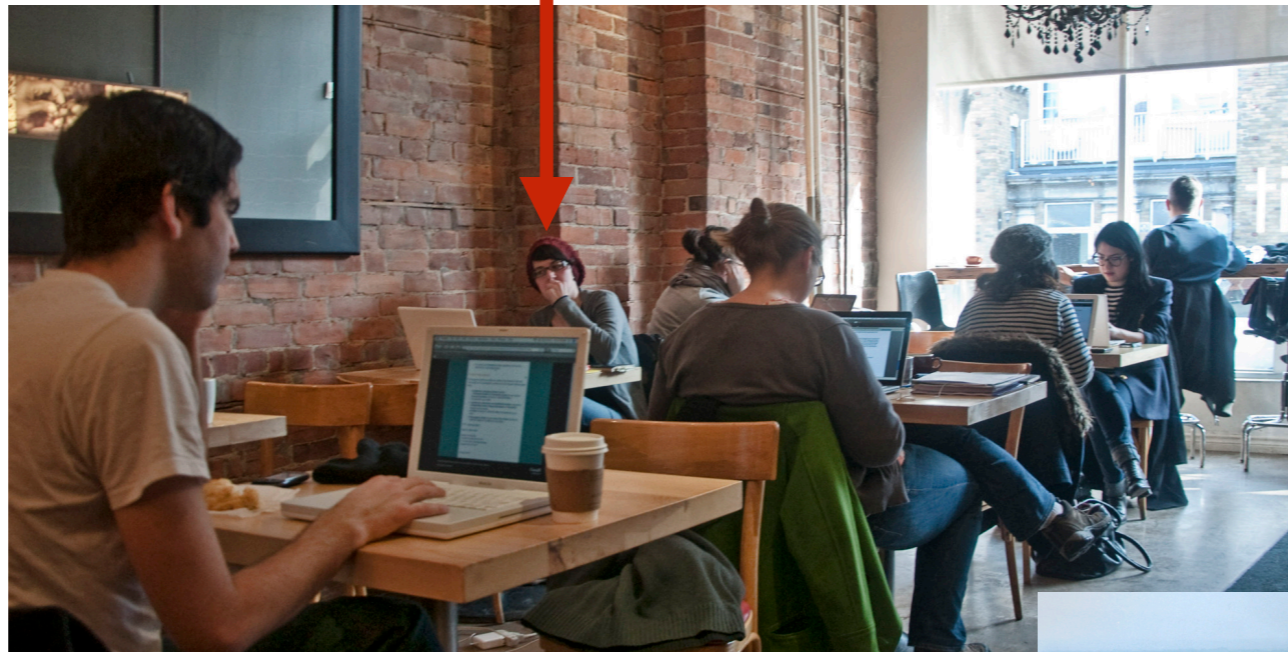
Bigger Q: What does “secure” even mean?

# Evaluating Security of Crypto

Kerckhoff's Principle: Assume adversary knows your algorithms and implementation. The only thing it doesn't know is the key.

1. Quantify adversary goals
  - Learn something about plaintext? Spoof a message?
2. Quantify adversary capabilities
  - View ciphertexts? Probe system with chosen inputs?
3. Quantify computational resources available to adversary
  - Compute cycles? Memory?





# International cyber crime ring smashed after more than \$530 million stolen



By Ben Westcott, CNN

Updated 2:09 AM ET, Thu February 8, 2018

