

# Recent and Future Trends in Cryptography

CMSC 23200/33250, Winter 2022, Lecture 25

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University of Chicago

# A Sampling of Recent and Future Trends in Crypto

1. End-to-End Messaging
2. Snowden Revelations
3. Homomorphic Encryption (+Post Quantum)
4. Zero-Knowledge Proofs + Password-Authenticated Key Exchange

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## **1. End-to-End Messaging**

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[Computing / Cybersecurity](#)

## Barr's call for encryption backdoors has reawakened a years-old debate

Attorney General William Barr's speech on Tuesday reignited a dispute that's more relevant than ever.

by Patrick Howell O'Neill

Jul 24, 2019



SECURITY  
WATCH

## US Attorney General William Barr Has Encryption All Wrong

*Attorney General William Barr has a completely wrong-headed take on encryption, and he's not the only one. Adding backdoors to secure services is a terrible idea, despite its popularity with law enforcement.*

By Max Eddy October 10, 2019



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# The U.K. Paid \$724,000 For A Creepy Campaign To Convince People That Encryption is Bad. It Won't Work.

BY [JOE MULLIN](#) | JANUARY 21, 2022

**DON'T GIVE**

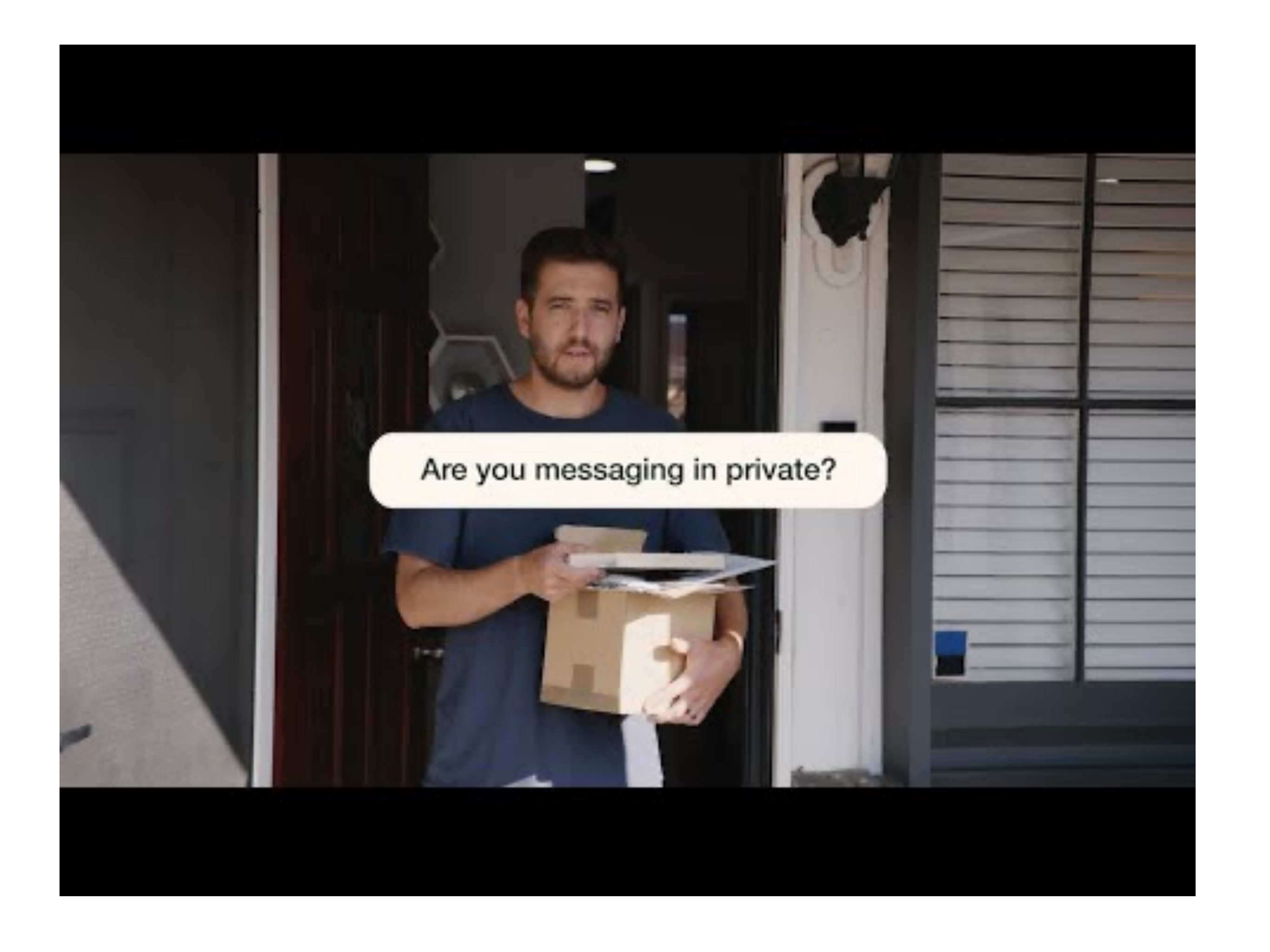
CHILD SEX ABUSERS

**A PLACE**

TO HIDE

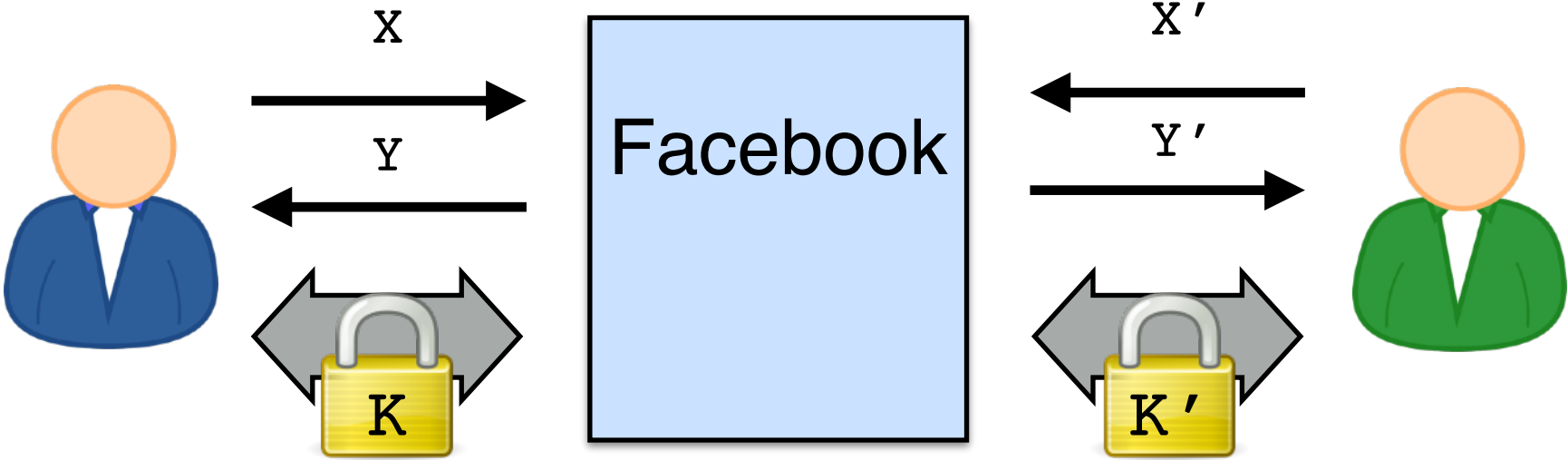
**Let's work together to ensure we keep children safe online without compromising user privacy**



A man with a beard and short dark hair, wearing a blue t-shirt, stands in a doorway. He is holding a cardboard box with both hands. The background shows the interior of a house and the exterior siding of a building. A white text box with rounded corners is overlaid on the image, containing the question "Are you messaging in private?".

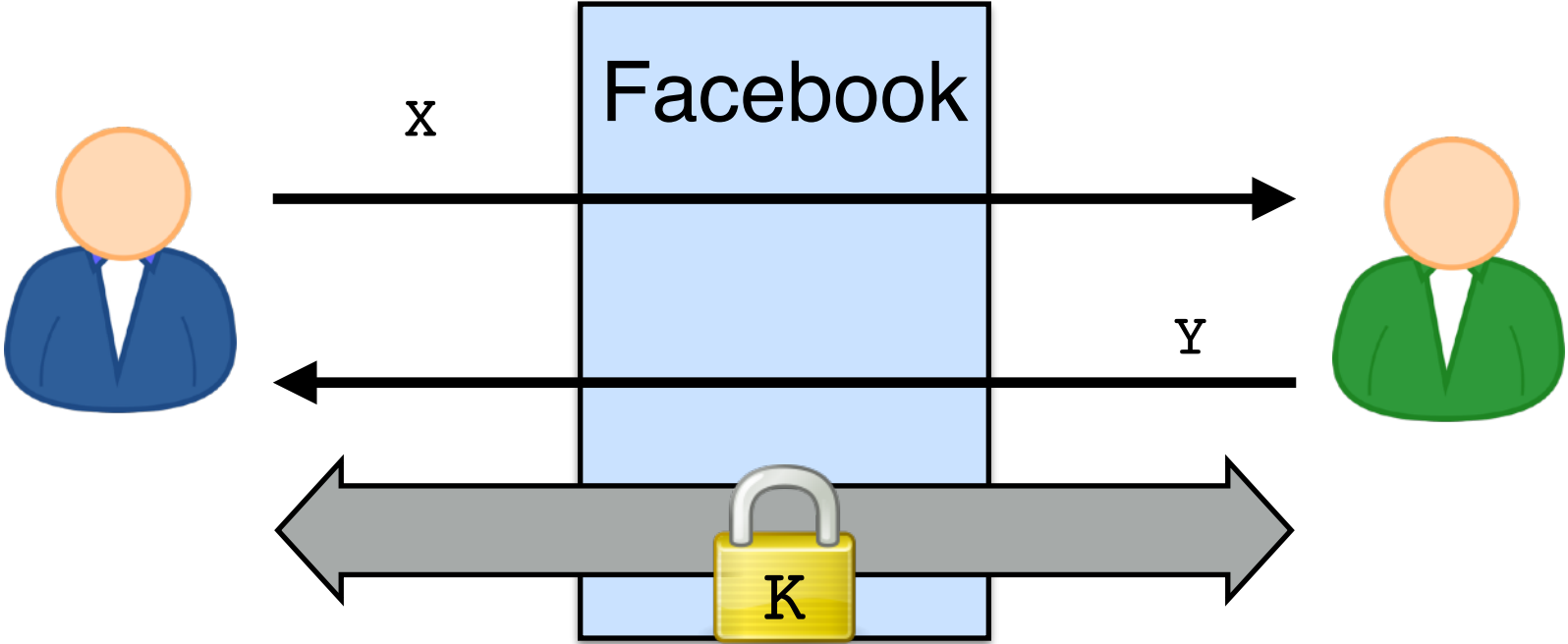
Are you messaging in private?

# Traditional Key Exchange Deployment (e.g. TLS)

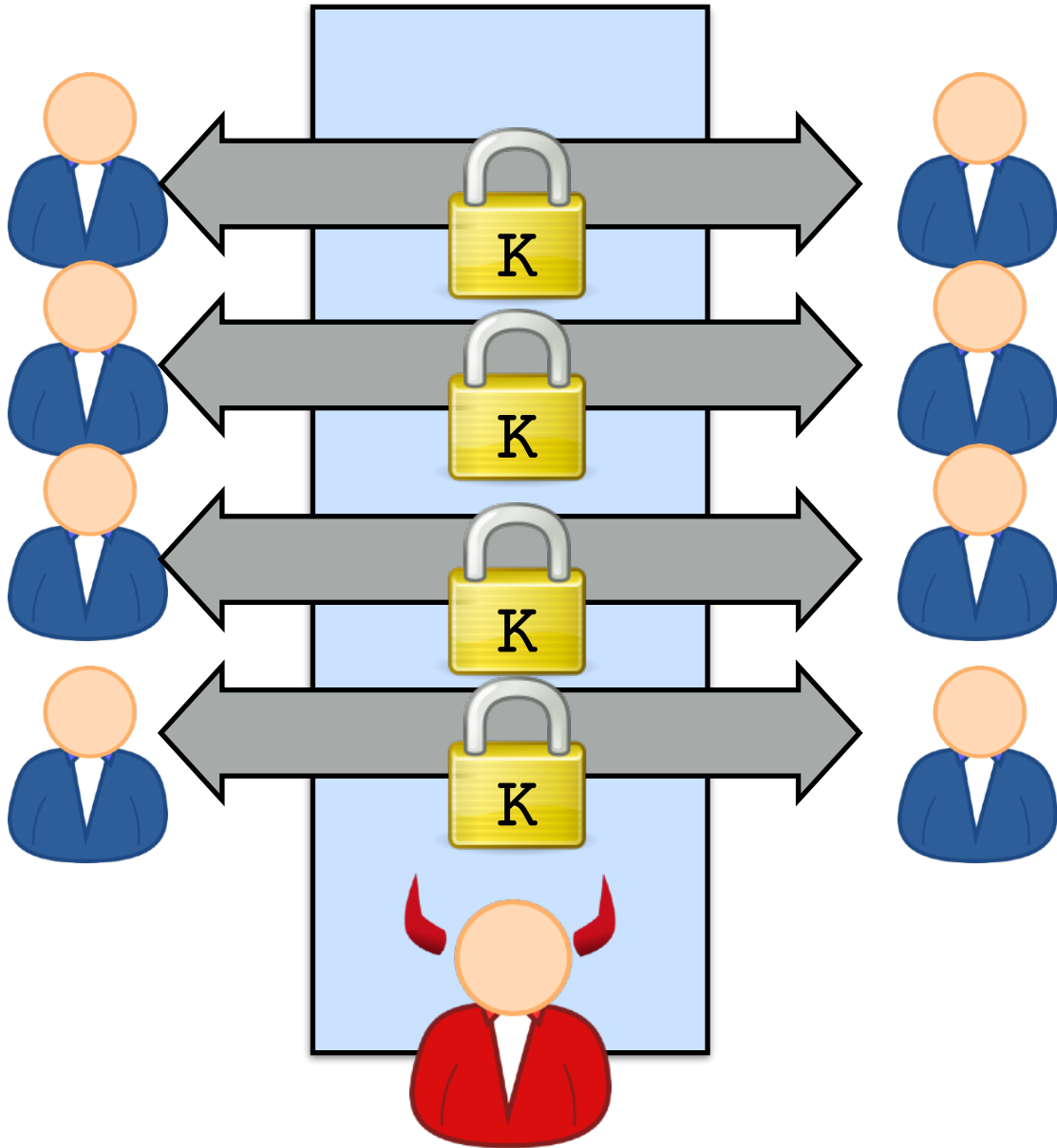
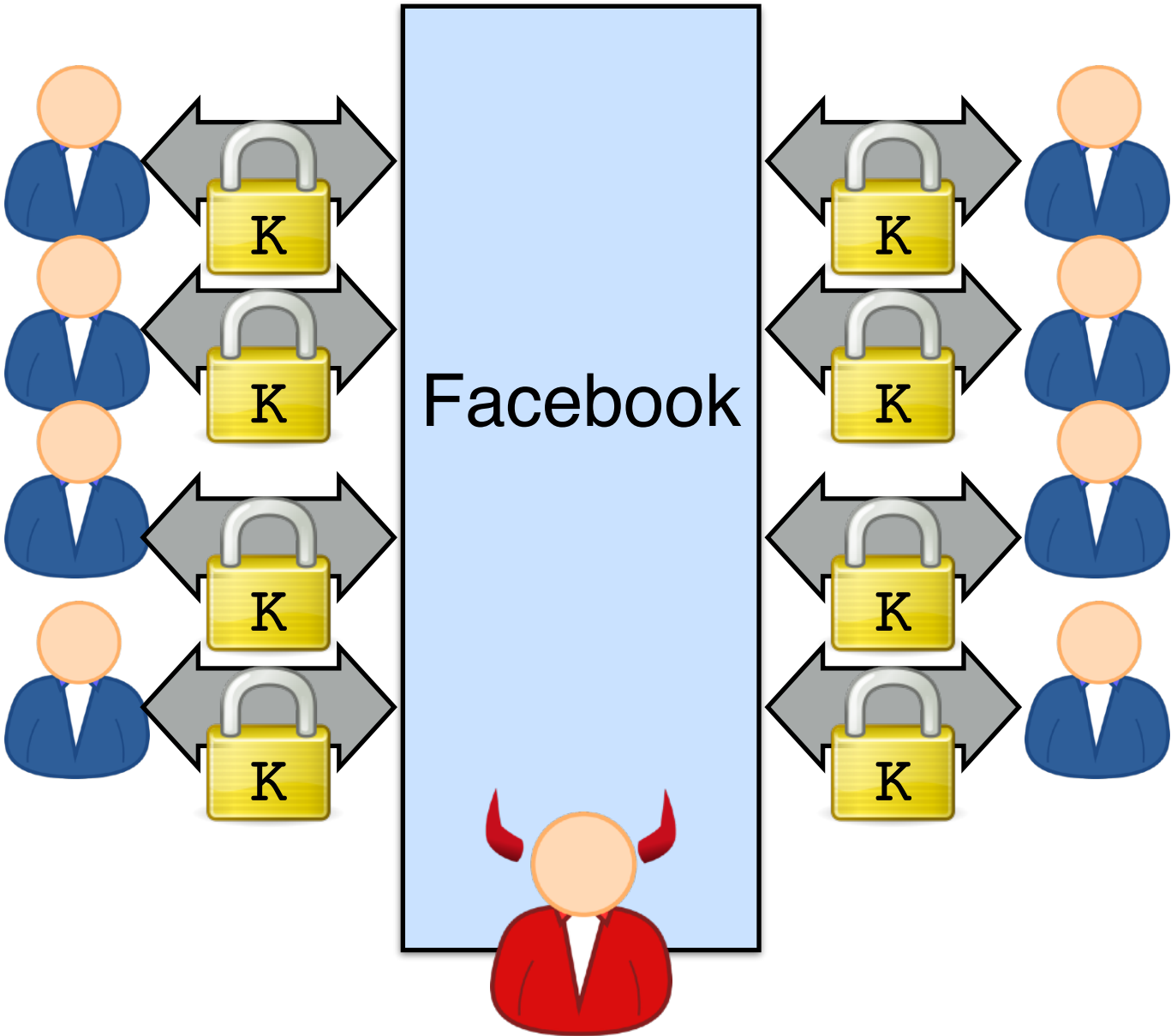




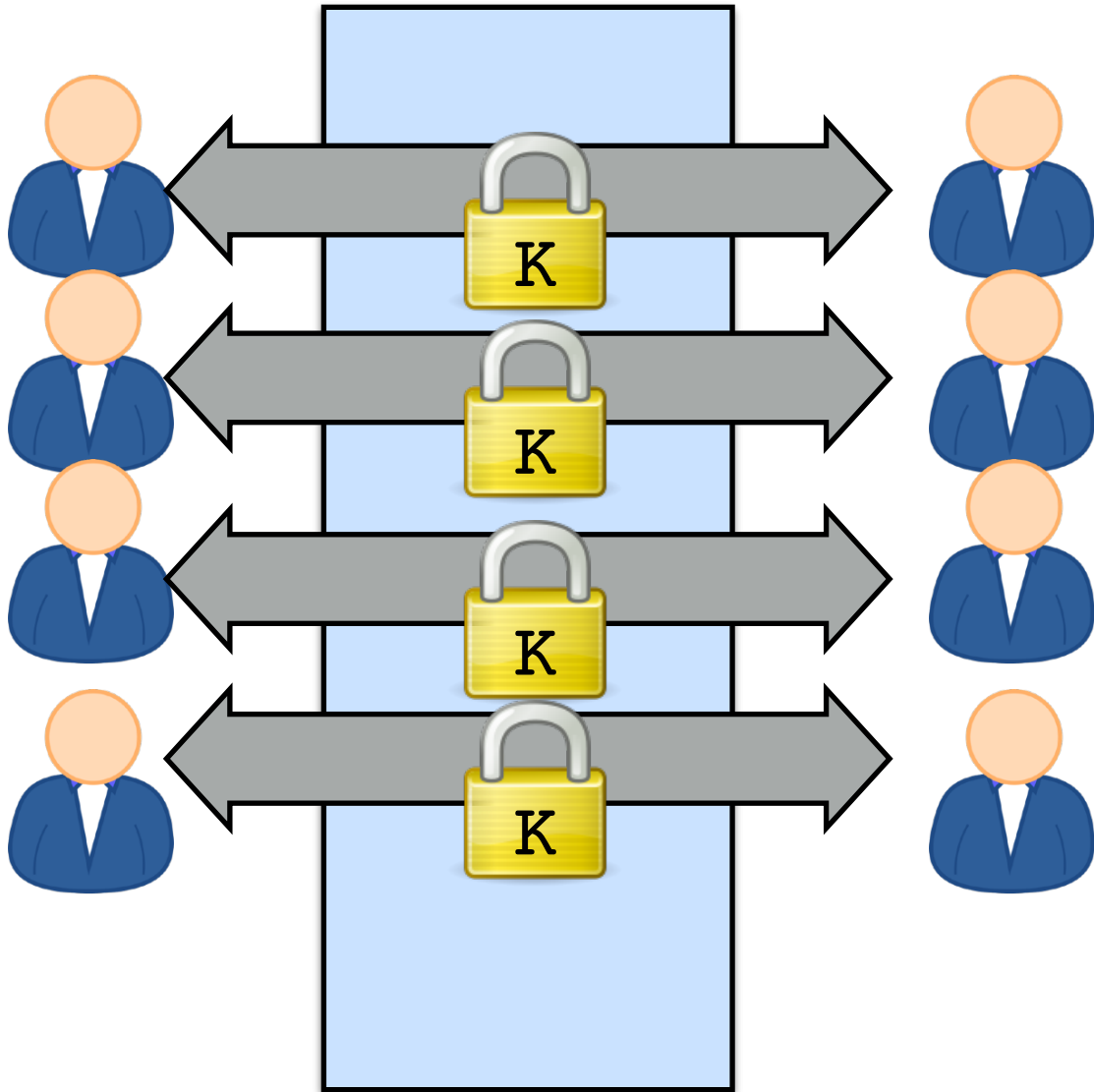
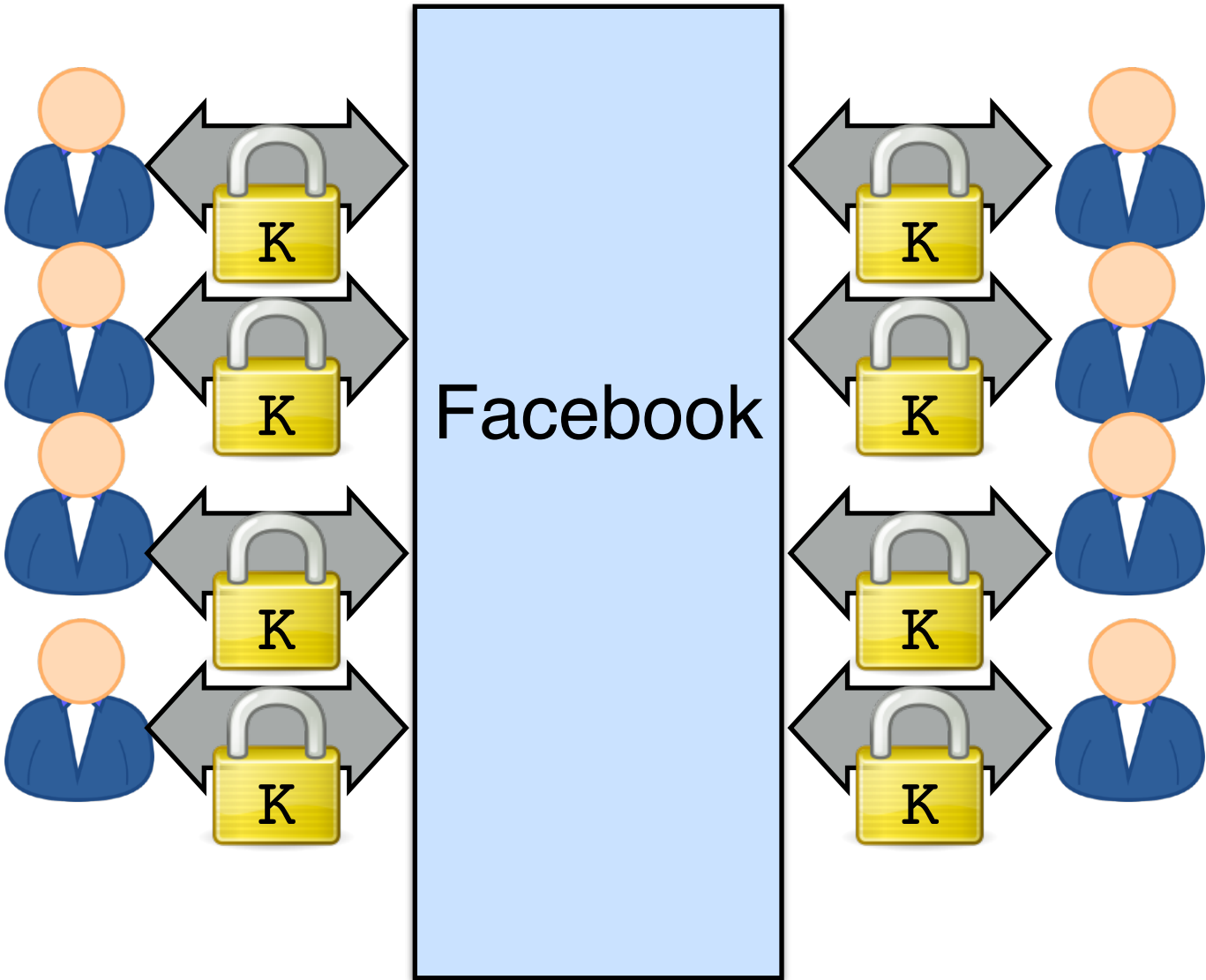
# End-to-End Key Exchange



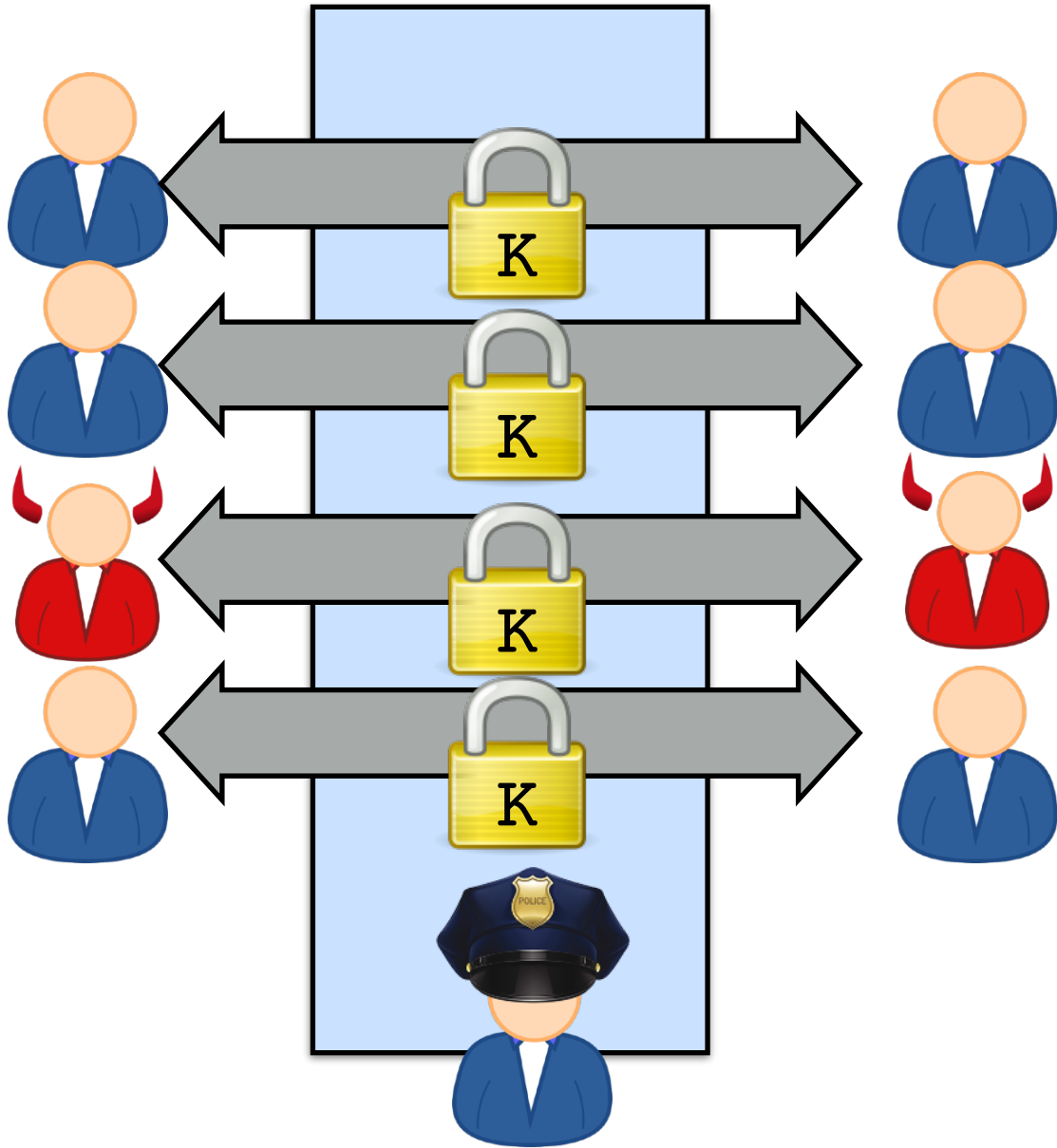
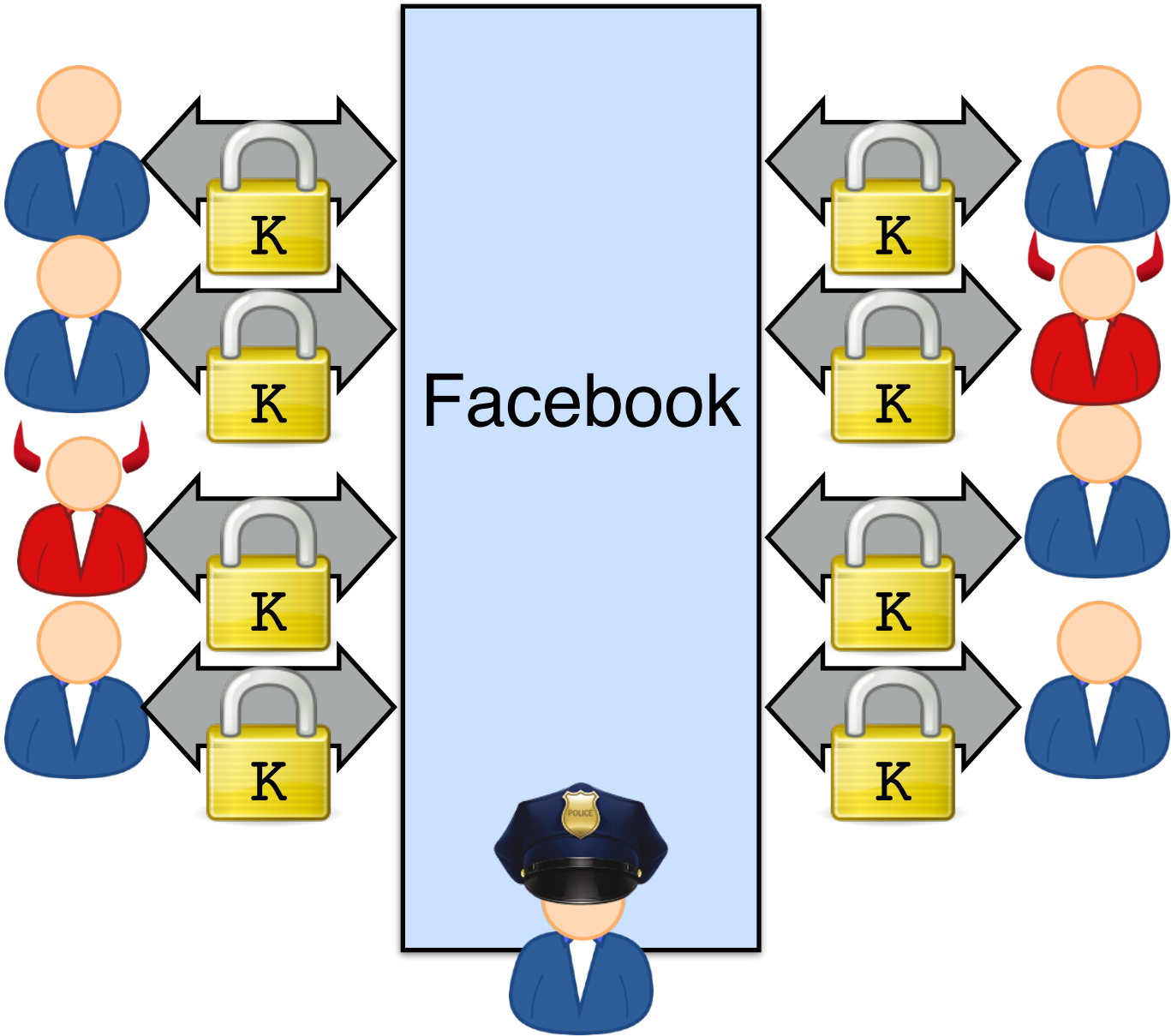
# Why End-to-End?



# Why *not* End-to-End?



# Why *not* End-to-End?



# Facebook: Don't expect full end-to-end encryption on Messenger until 2022 'at the earliest'



by **Owen Hughes** in **Security**   
on May 4, 2021, 8:35 AM PDT

Facebook says it wants to make E2EE the default across all of its messaging platforms, but this will be a gradual process.

**WHITE PAPERS, WEBCASTS, AND  
DOWNLOADS**



Reduce your Networks  
Attack Surface with Zero  
Trust Network Access

# Google will let enterprises store their Google Workspace encryption keys

**Zack Whittaker** @zackwhittaker / 5:00 AM CDT • June 14, 2021

 Comment

As ubiquitous as Google Docs has become in the last year alone, a major criticism often overlooked by the countless workplaces that use it is that it isn't end-to-end encrypted, allowing Google — or any requesting government agency — access to a company's files. But Google is finally addressing that key complaint with a round of updates that will let customers shield their data by storing their own encryption keys.

Google Workspace, the company's enterprise offering that includes Google Docs, Slides and Sheets, is adding client-side encryption so that a company's data will be indecipherable to Google.



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5. ORAM (Alex)

# The Snowden Revelations



## 2013 Snowden Revelations Included:

1. Collected millions of images from Yahoo! messenger to build facial recognition system (2008-2010)
2. Recorded audio of *every* call in the Bahamas (2009-?)
3. Tapped internal lines for Google and Yahoo! data centers
4. Likely built a crypto backdoor into a NIST algorithm, then paid a company \$10 million to use that algorithm



BIZ & IT —

# NSA official: Support of backdoored Dual\_EC\_DRBG was “regrettable”

Agency supported crypto function for years after "trap door" was disclosed.

DAN GOODIN - 1/14/2015, 12:43 PM



WIRED

SUBSCRIBE

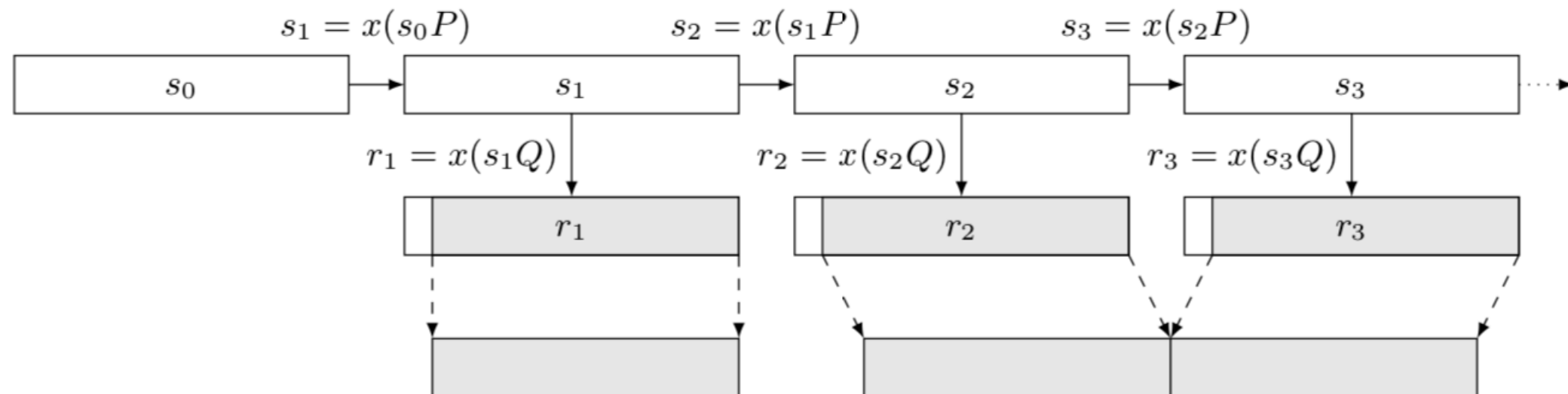
KIM ZETTER

SECURITY 09.24.13 06:30 AM

## How a Crypto 'Backdoor' Pitted the Tech World Against the NSA

# Dual\_EC\_DRBG: A Pseudorandom Generator

**Pseudorandom generator:** Algorithm for “stretching” a random string.



NIST Special Publication 800-90A

**Recommendation for Random Number  
Generation Using Deterministic  
Random Bit Generators**

Elaine Barker and John Kelsey

Computer Security Division  
Information Technology Laboratory

From: John Kelsey [mailto:john.kelsey@nist.gov]  
Sent: Wednesday, October 27, 2004 11:17 AM  
To: Don Johnson  
Subject: Minding our Ps and Qs in Dual\_EC

Do you know where Q comes from in Dual\_EC\_DRBG?

Thanks,

-John



Subject: RE: Minding our Ps and Qs in Dual\_EC  
From: "Don Johnson"  
Date: Wed, October 27, 2004 11:42 am  
To: "John Kelsey"

John,

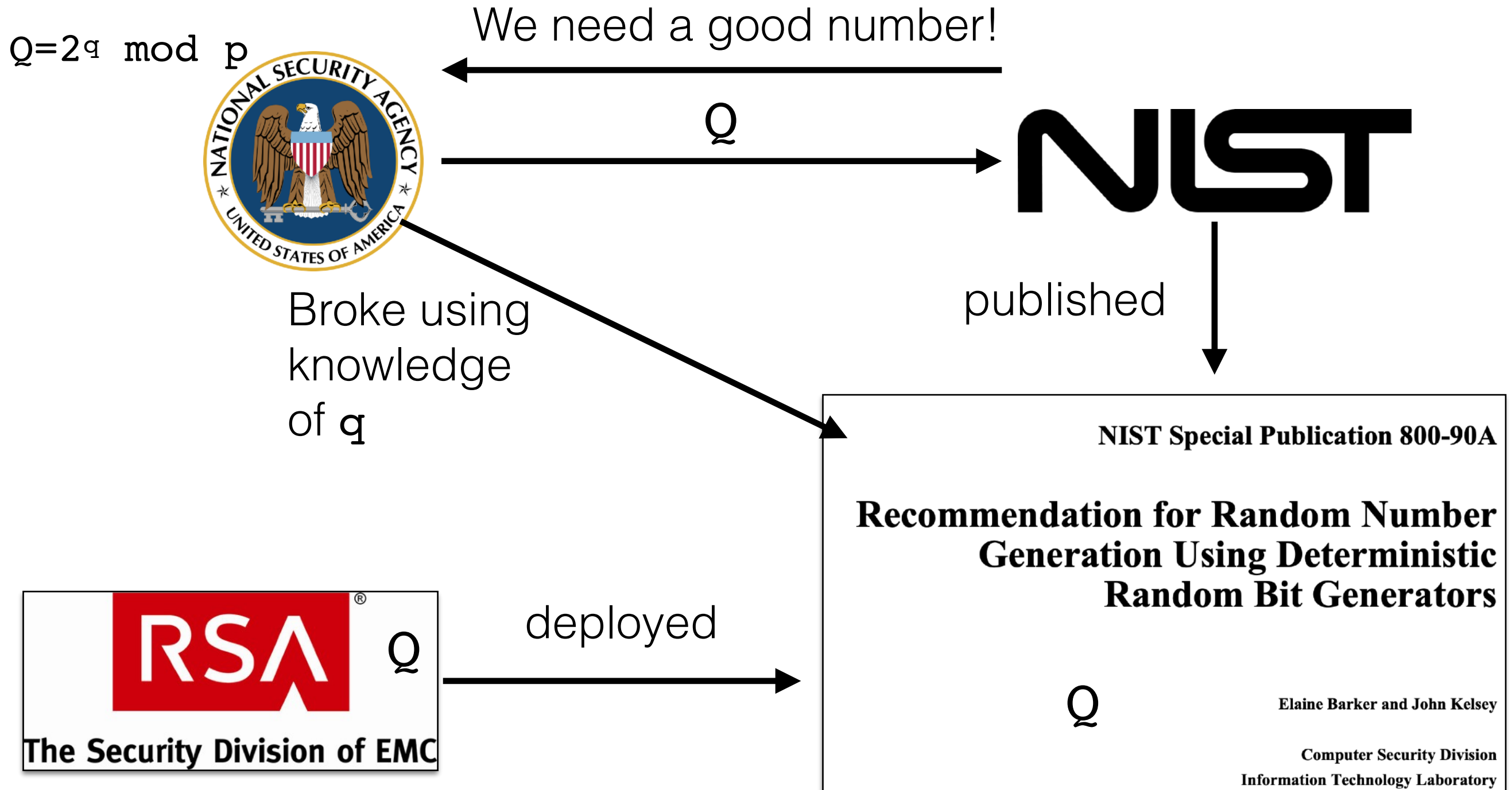
P=G.

Q is (in essence) the public key for some random private key.

It could also be generated like a(nother) canonical G, but NSA kyboshed this idea, and I was not allowed to publicly discuss it, just in case you may think of going there.

Don B. Johnson

# Dual\_EC\_DRBG Development Process\*



\*Actual math is over elliptic curves, and attack is complicated!

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# Malleable Encryption

$C \leftarrow \text{Enc}(\text{PK}, M)$



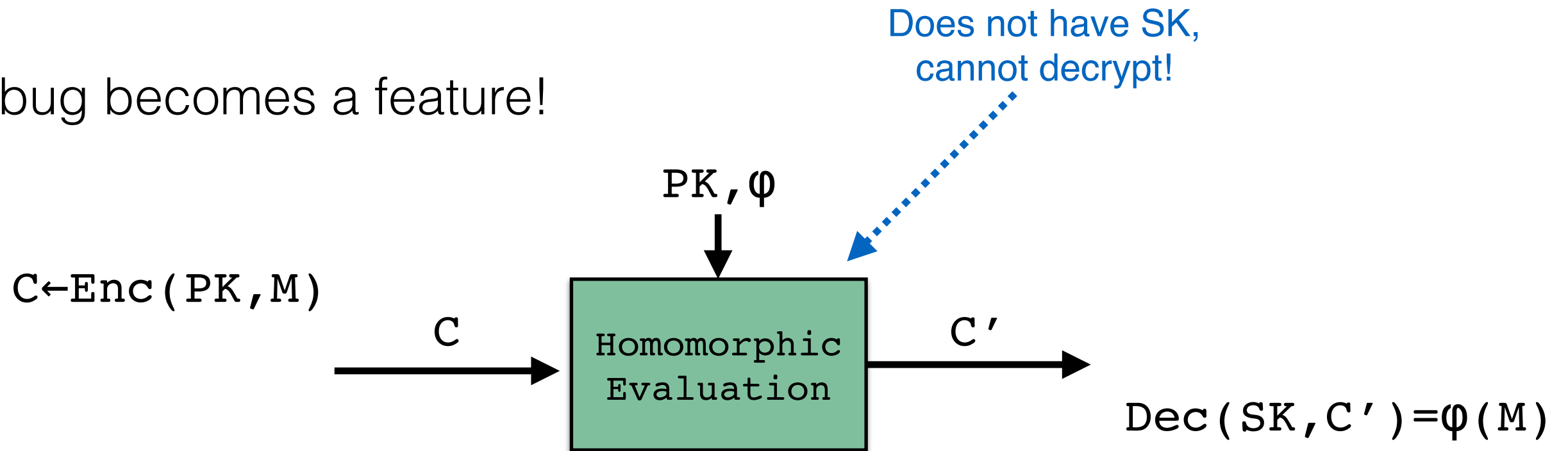
$\text{Dec}(\text{SK}, C' \bmod N) = M * x$

$$C' \leftarrow [ (x^e) * C \bmod N ]$$

- Malleability is usually a bad thing for Plain RSA Enc/Signatures
- Allows adversaries to predictably change plaintexts without permission, and without even knowing the original message

# Homomorphic Encryption = Very Malleable Encryption

- A bug becomes a feature!



- RSA is homomorphic for multiplication by some fixed  $x$ :

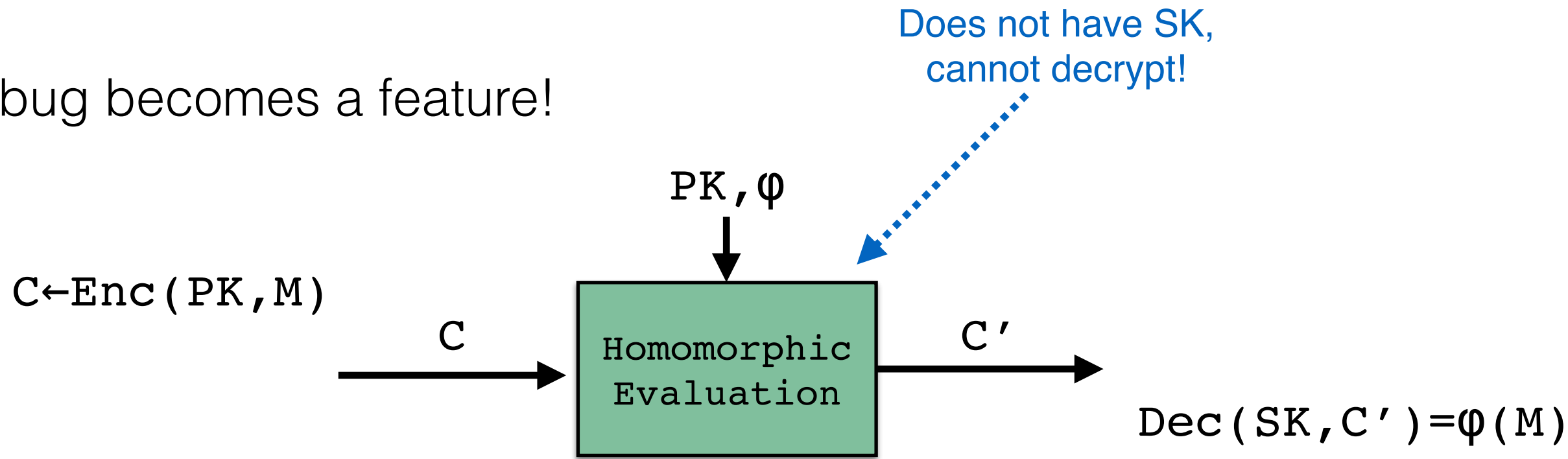
$$\varphi_x(M) = (x * M \bmod N)$$

- RSA does not appear to homomorphic for *addition* by some fixed  $x$ :

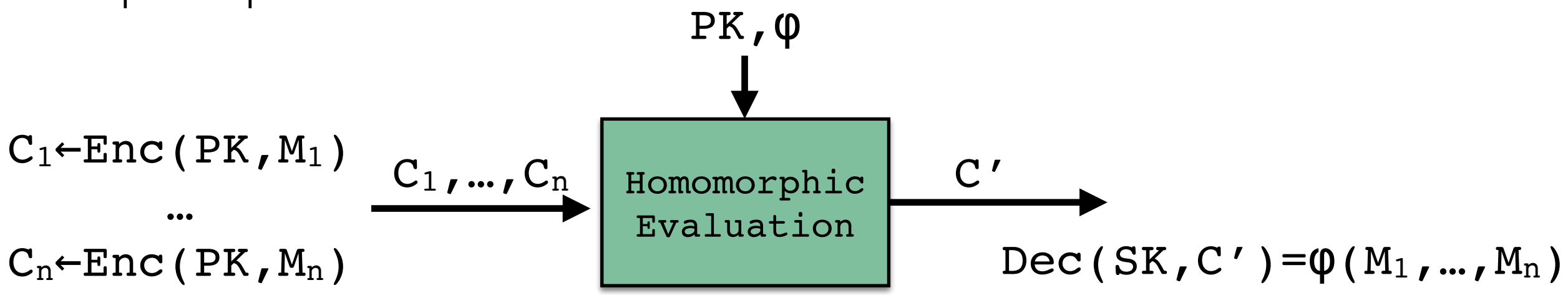
$$\varphi_x(M) = (x + M \bmod N) ???$$

# Homomorphic Encryption = Very Malleable Encryption

- A bug becomes a feature!



- Multiple-ciphertext version:





# Homomorphic Encryption: The Grand Vision (1978)

## ON DATA BANKS AND PRIVACY HOMOMORPHISMS

*Ronald L. Rivest*  
*Len Adleman*  
*Michael L. Dertouzos*

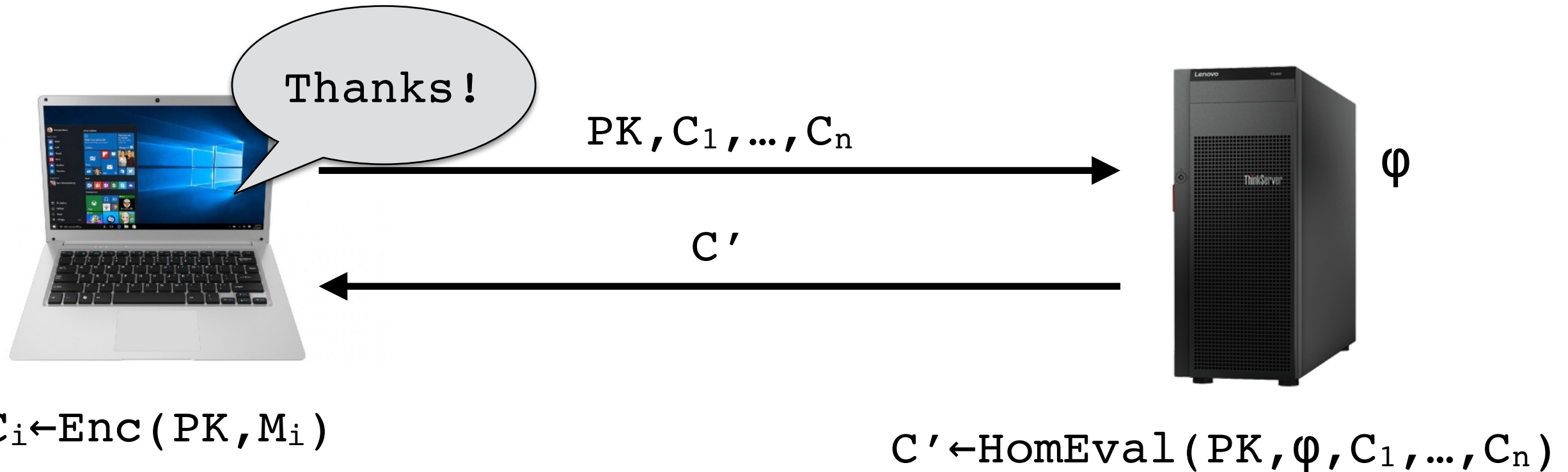
Massachusetts Institute of Technology  
Cambridge, Massachusetts

### I. INTRODUCTION

Encryption is a well-known technique for preserving the privacy of sensitive information. One of the basic, apparently inherent, limitations of this technique is that an information system working with encrypted data can at most store or retrieve the data for the user; any more complicated operations seem to require that the data be decrypted before being operated on.

# Homomorphic Encryption: The Grand Vision (1978)

- Suppose  $\text{Enc}$  is homomorphic for  $\phi$  using  $\text{HomEval}$

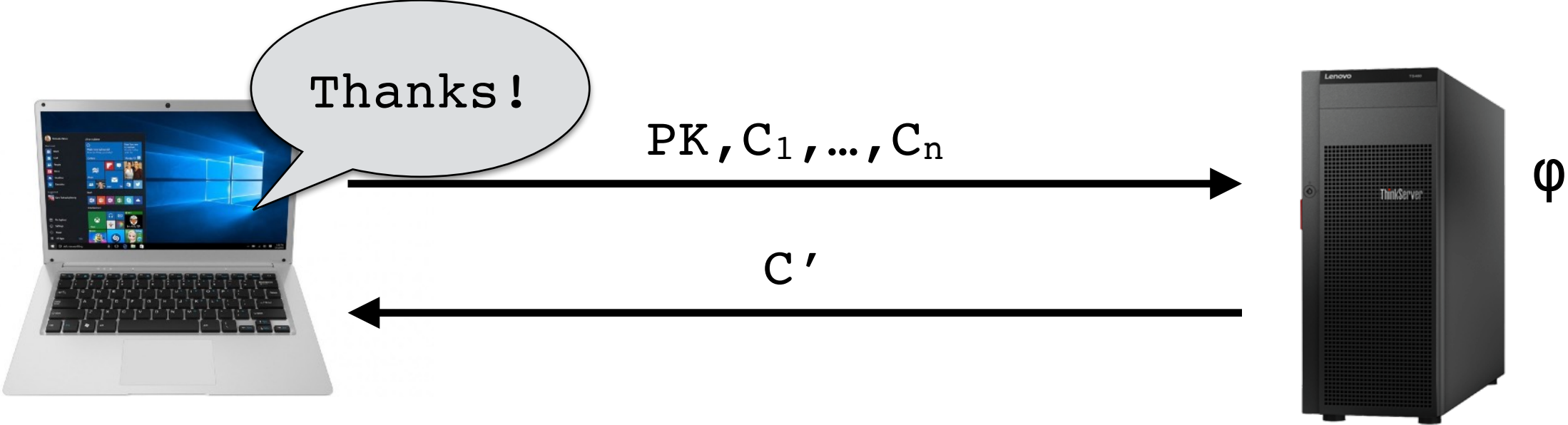


$$\phi(M_1, \dots, M_n) \leftarrow \text{Dec}(SK, C')$$

- Client learns  $\phi$  applied to its own data  $M_1, \dots, M_n$
- Client does not learn  $\phi$
- Server does not learn  $M_1, \dots, M_n$

# Homomorphic Encryption: The Grand Vision (1978)

- Suppose Enc is homomorphic for  $\phi$  using HomEval



$$C_i \leftarrow \text{Enc}(PK, M_i)$$

$$\phi(M_1, \dots, M_n) \leftarrow \text{Dec}(SK, C')$$

- Train private machine-learning models
- Run expensive simulations
- Query databases without decrypting

- Client learns  $\phi$  applied
- Client does not learn  $\phi$
- Server does not learn  $M_1, \dots, M_n$

# For which $\varphi$ can we build homomorphic encryption?

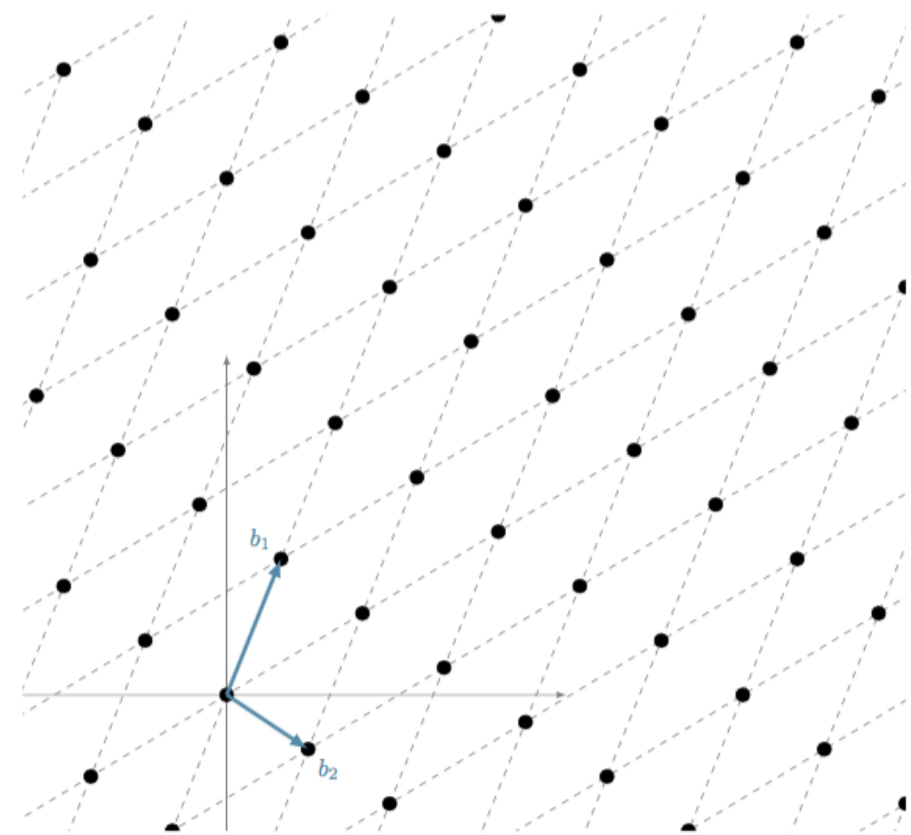
- RSA ('78):  $\varphi$  = multiplication mod  $N$  of plaintexts and/or constants
- Paillier ('99):  $\varphi$  = *addition mod  $N$*  of plaintexts and/or constants
- ...

**Observation:** If an encryption is homomorphic for both additions and multiplications mod  $N$ , then it is homomorphic for any  $\varphi$ !

- BGN ('06):  $\varphi$  = many additions but only one multiplication
- ...
- Gentry ('09): Any  $\varphi$ ! Via new techniques.

# Homomorphic Encryption and Lattices (Gentry'09)

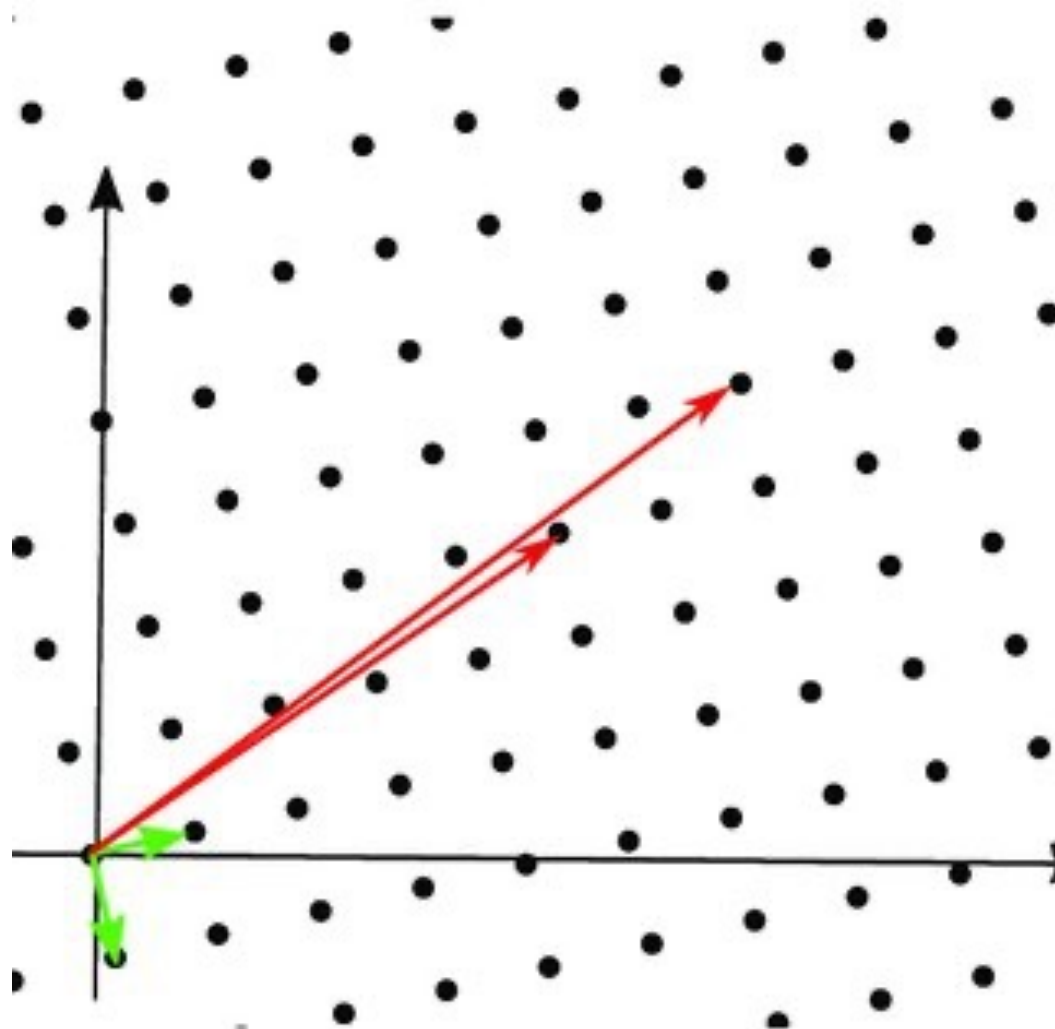
- Based on different math (not RSA/Diffie-Hellman)
- Uses *lattices*, i.e. high-dimension integer grids
- Original construction was too slow
- Tons of research on making it faster



# Underlying Hard Problem: Shortest Vector Problem

**Input:** An  $n$ -by- $m$  integer matrix  $\mathbf{B}$  ( $m < n$ )

**Output:** The smallest non-zero  $\mathbf{y}$  such that  $\mathbf{B}\mathbf{x}=\mathbf{y}$  for some integer  $\mathbf{x}$ .



- Easy for small  $n$
- Appears hard for large  $n$ ...
- Even for quantum computers!

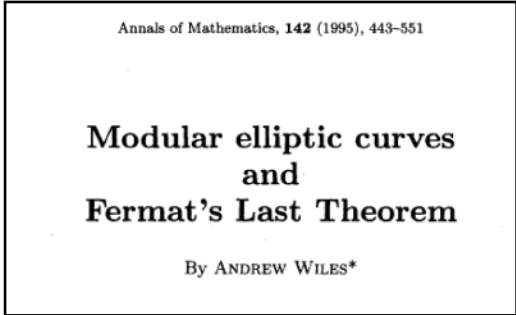
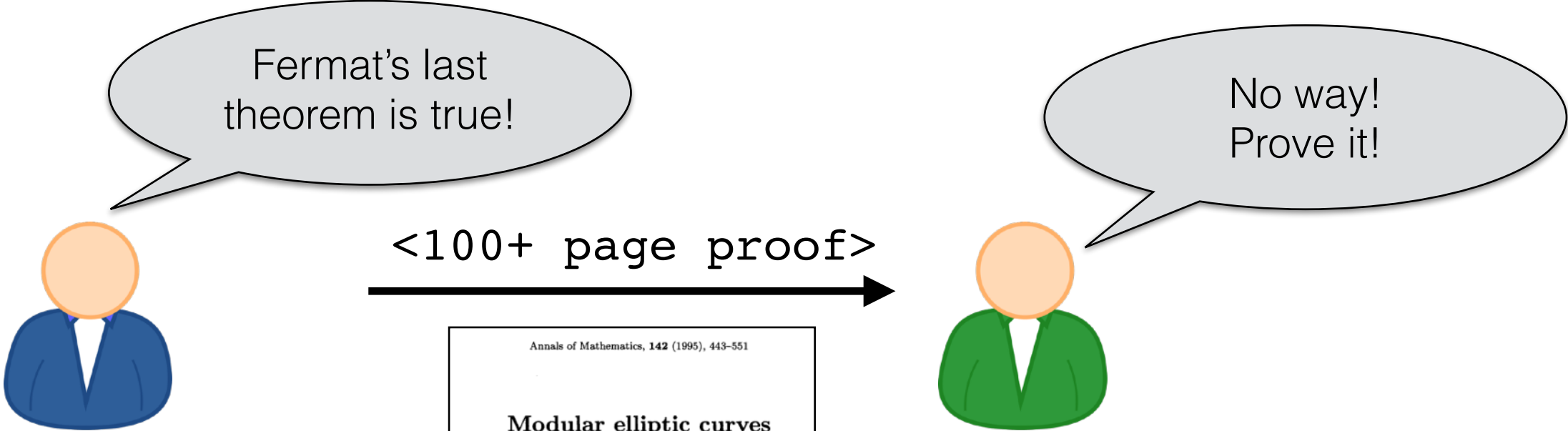
A screenshot of the NIST Information Technology Laboratory website. The header includes the NIST logo and the text "Information Technology Laboratory". Below this is a blue banner with the text "COMPUTER SECURITY RESOURCE CENTER". Underneath the banner are two green buttons labeled "PROJECTS" and "POST-QUANTUM CRYPTOGRAPHY". The main content area features the text "Post-Quantum Cryptography PQC" and social media icons for Facebook and Twitter.



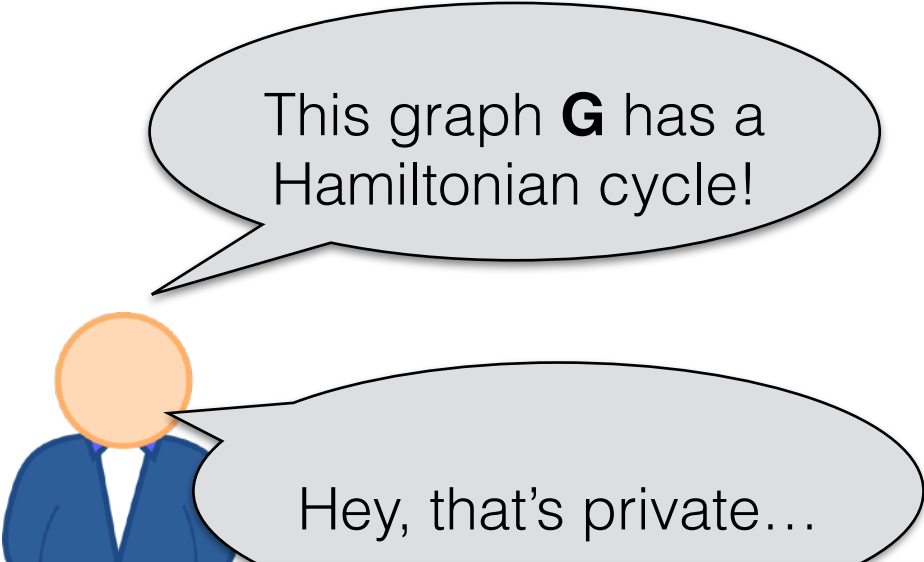
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# Switching gears: Mathematical Proofs



- Convinced theorem is true
- Learns *why it's true* (i.e. because all semi-stable curves are modular...)

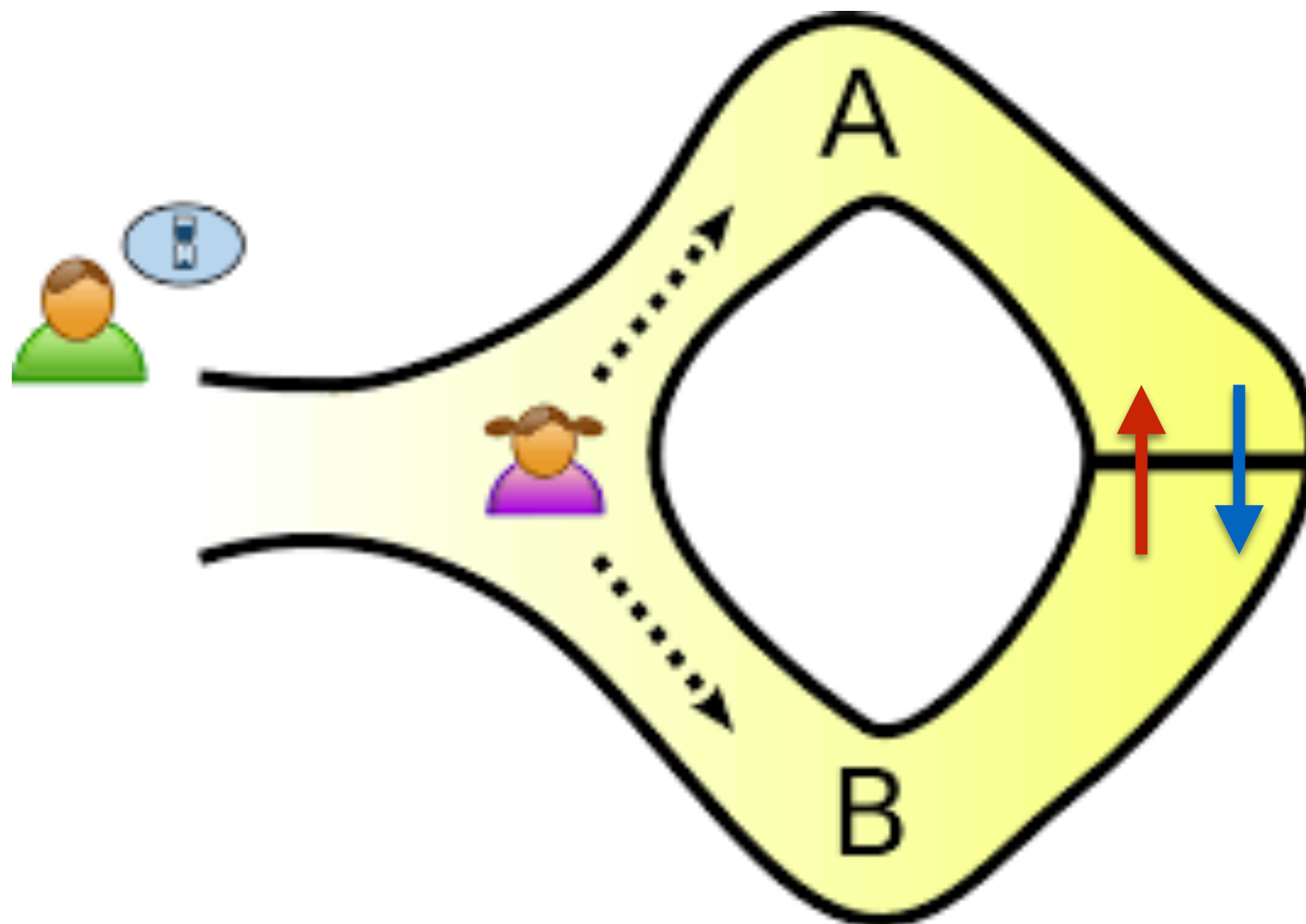


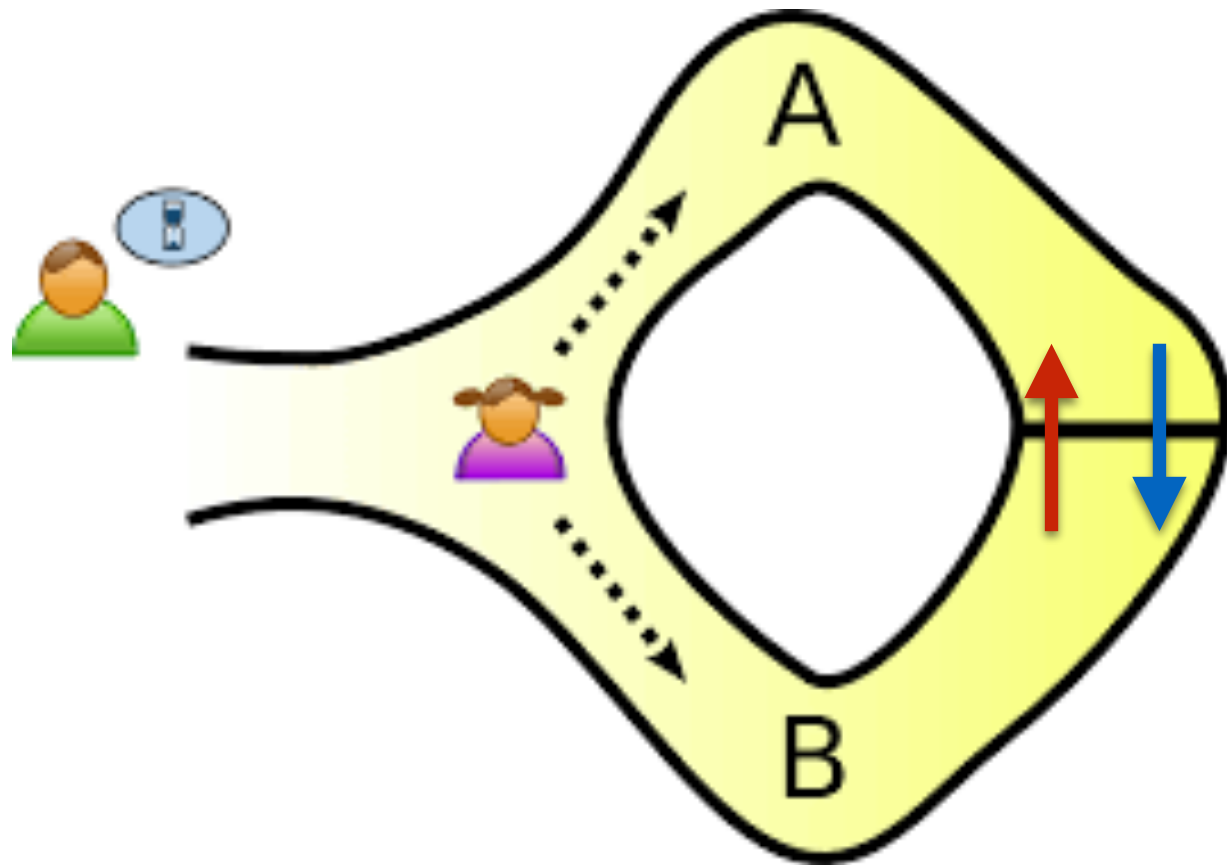
Question: Can one prove something is true...  
...without revealing anything about why?

# Zero-Knowledge Proofs (Goldwasser, Micali, Rackoff '85)



- Prover claims: There is a one-way door that opens between A and B
- Wants to hide: Which direction the door opens ( $A \rightarrow B$  vs  $B \rightarrow A$ )





### Protocol:

1. Prover walks into cave without Verifier watching
2. Verifier flips a coin and asks Prover to come out A or B side
3. Prover comes out that side, using door if necessary
4. Repeat 100 times. If prover is ever caught lying, **REJECT**.

**Soundness:** If there is (in fact) no door, then Prover only has  $1/2^{100}$  chance to cheat.

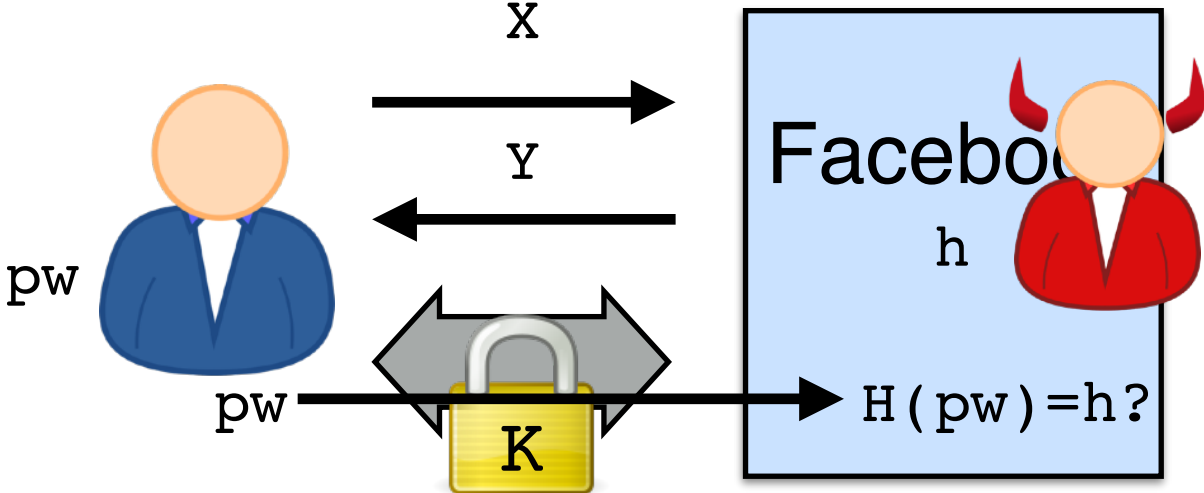
**Zero-knowledge:** Even if Verifier tries to cheat, it won't learn anything about which way the door opens.

- Key insights:
  - Interaction
  - Randomness

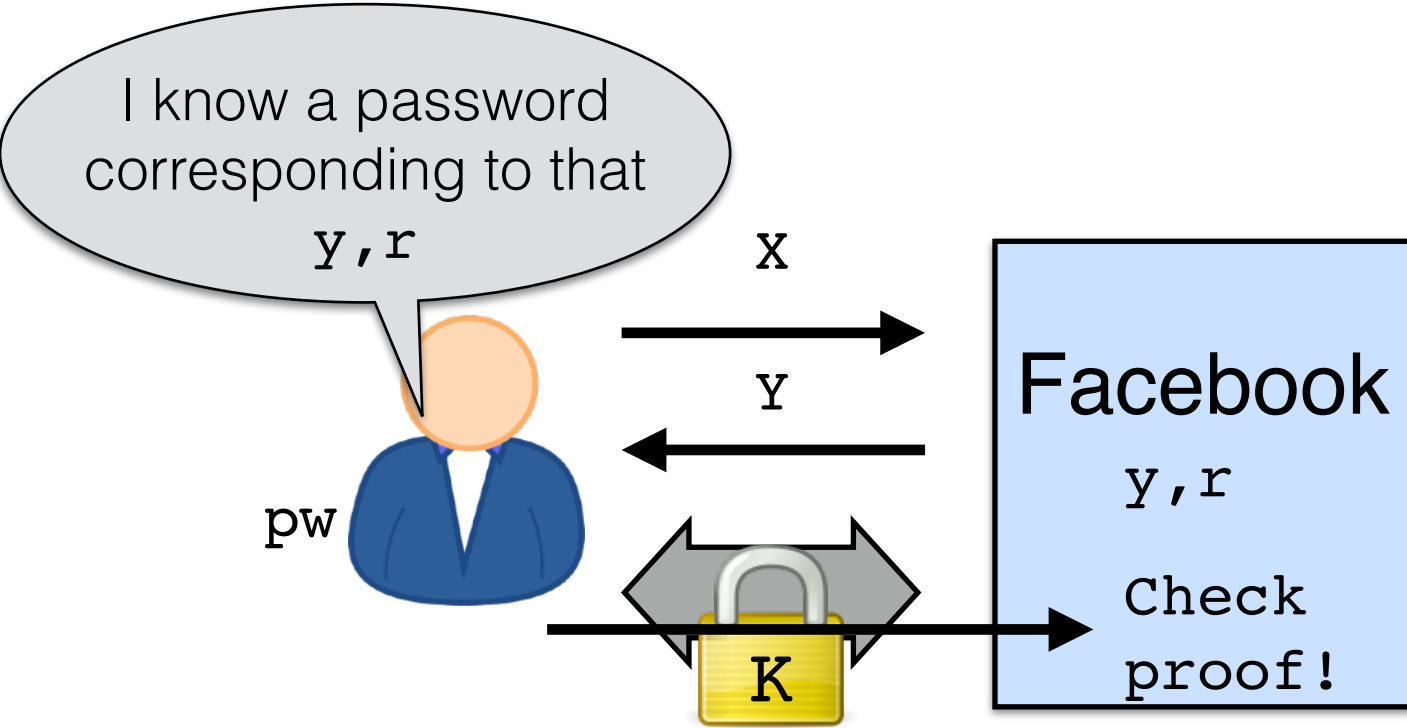
# Application: Password-Authenticated Key Exchange

The screenshot shows the top portion of a Cloudflare blog article. At the top left is the Cloudflare logo, followed by the text 'The Cloudflare Blog'. On the top right, there is a navigation link 'Thanks for being here, come' and an email subscription input field labeled 'Email Address'. Below the header is a horizontal menu with categories: 'Product News', 'Speed & Reliability', 'Security', 'Serverless', 'Cloudflare Network', 'Developers', and 'Deep Dive'. The main content area features a large, bold title 'OPAQUE: The Best Passwords Never Leave your Device'. Below the title is the date '12/08/2020' and a circular profile picture of the author, Tatiana Bradley, with her name written next to it.

# Application: Password-Authenticated Key Exchange



- Hash stored at FB.
- Compromise at server allows stealing pw, even if very strong



- pw never sent to FB, even at registration
- Compromise at server won't allow stealing pw (assuming it is strong)

What are the downsides?

The End